

# Virtual Process Design for Coupled Quasi-Static and Electromagnetic Forming

Marco Rozgić and Marcus Stiemer

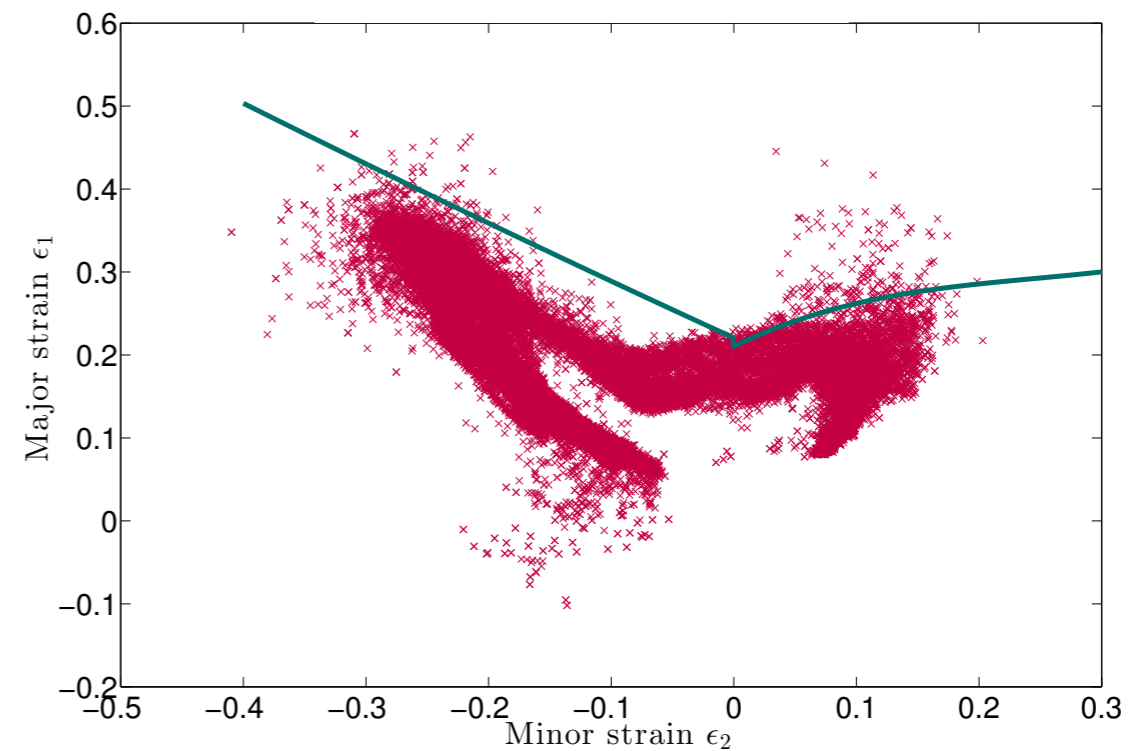
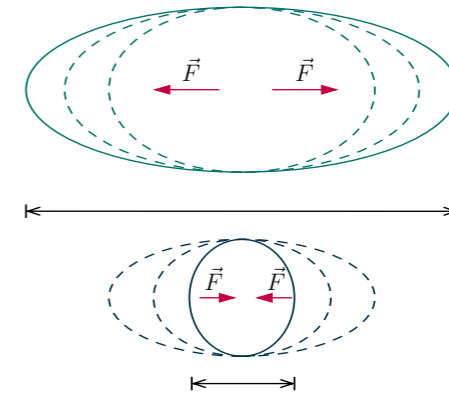
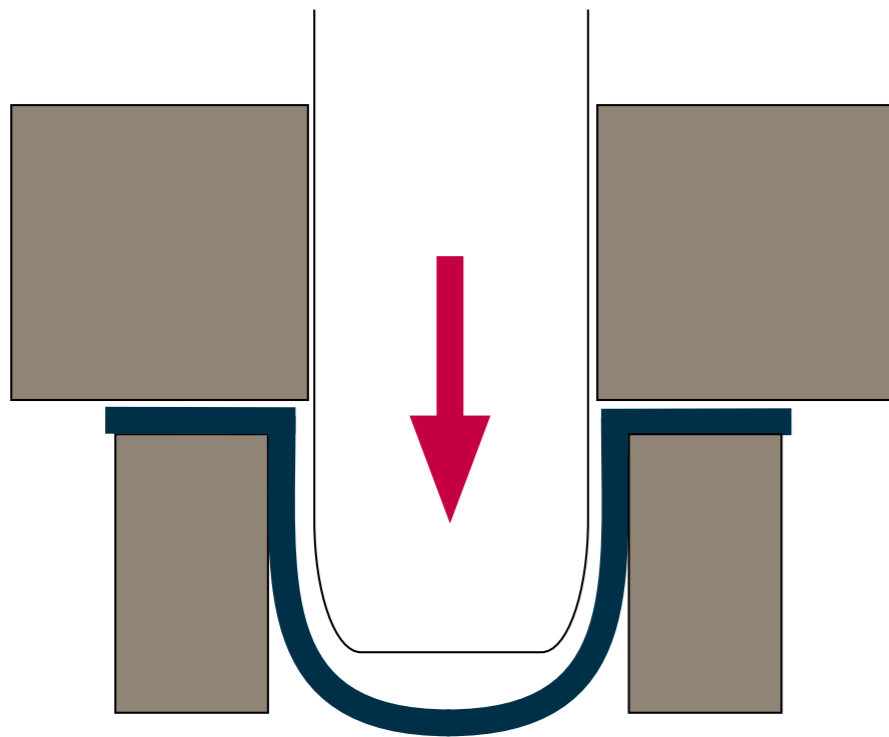


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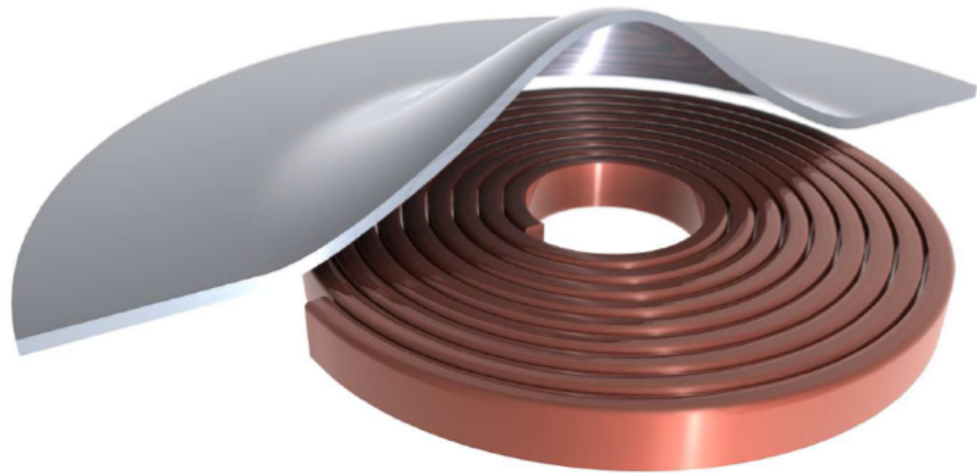


# Quasi-Static Forming

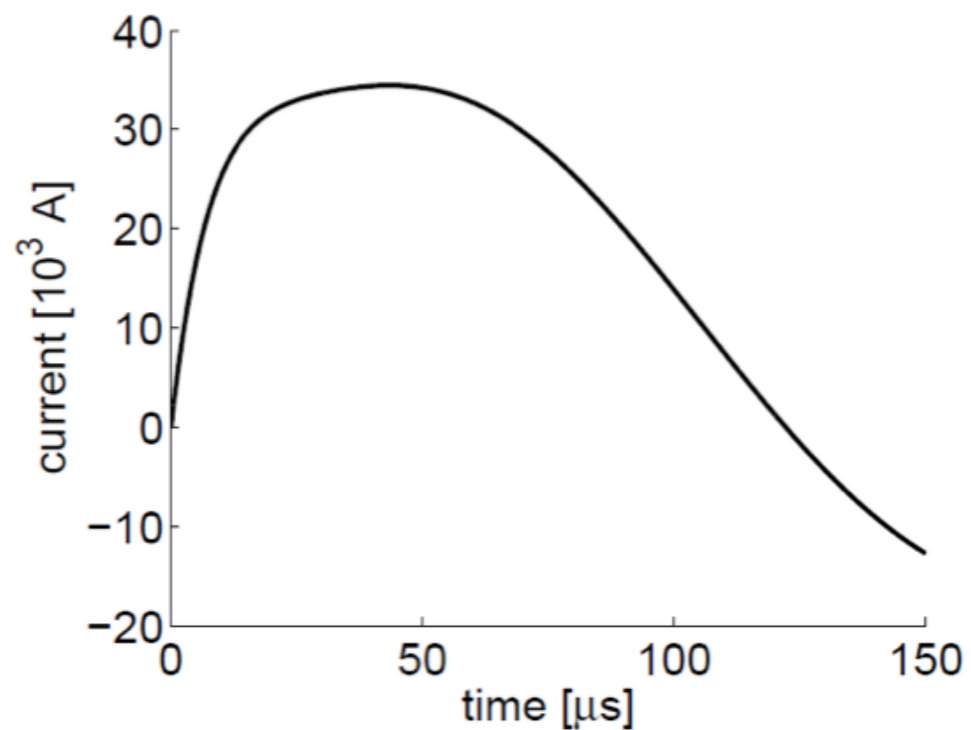


- Quasi-static forming is restricted by the **forming limit**
- Forming beyond limit is possible by **high speed forming**

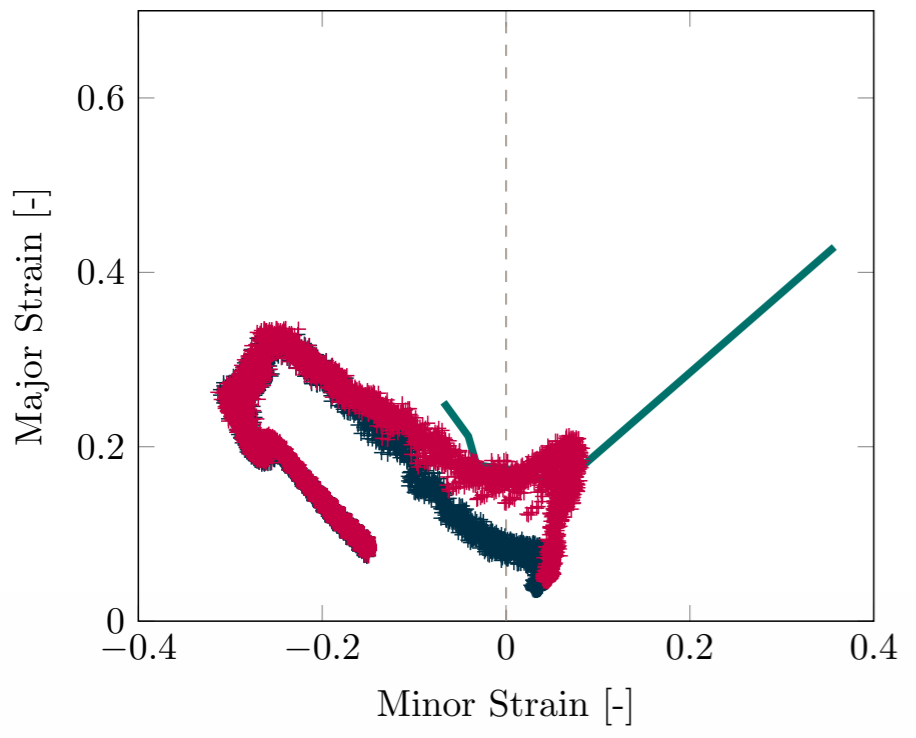
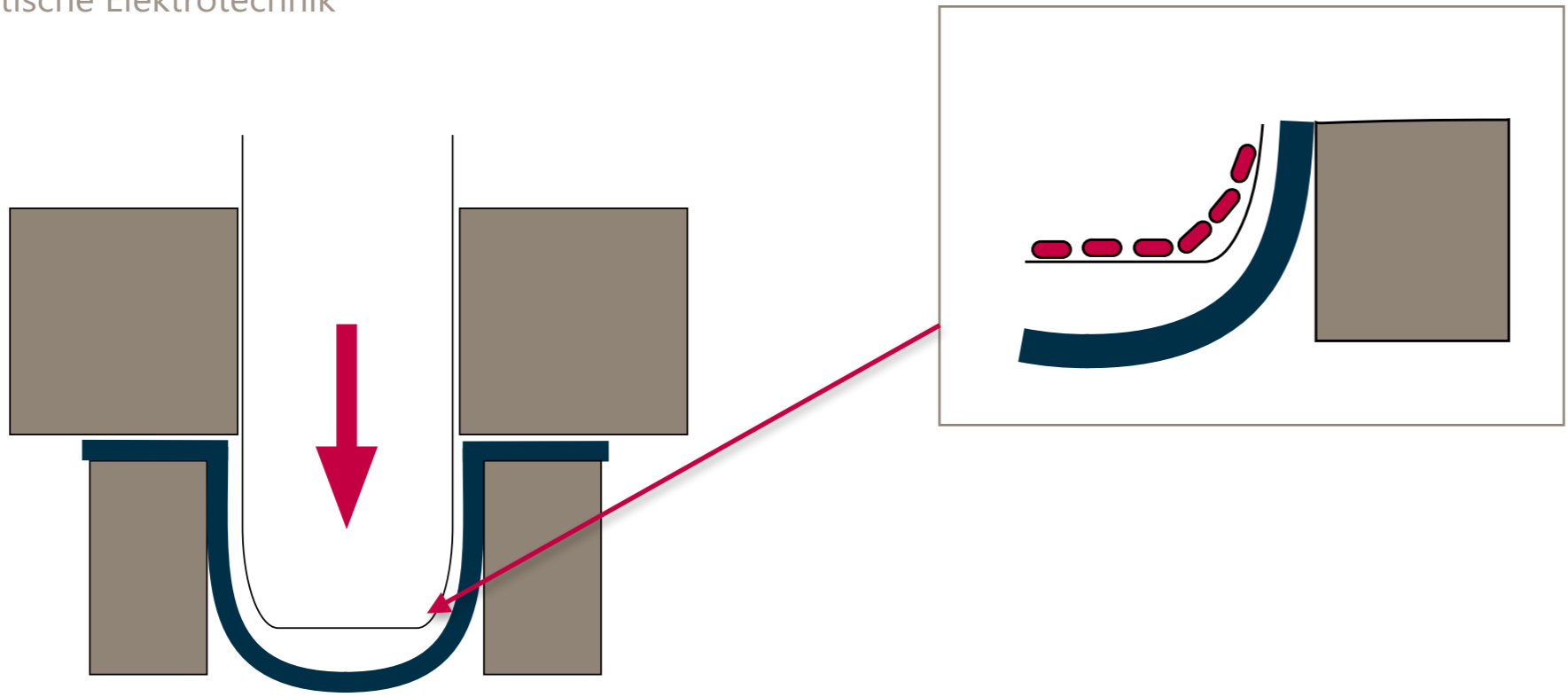
# Electromagnetic Impulse Forming



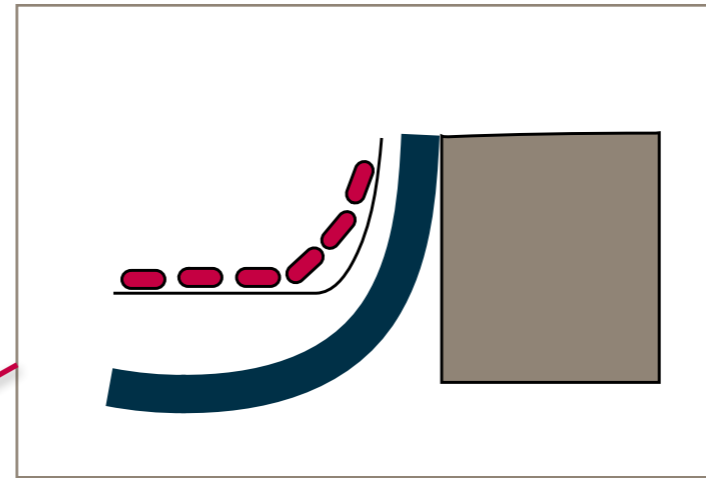
- Electromagnetic impulse forming with pulsed currents (e.g. 30kA within 10 $\mu$ s)  
→ magnetic flux between tool coil and workpiece: 1-10 Tesla
- Induced current results in **Lorentz forces**  
→ forming



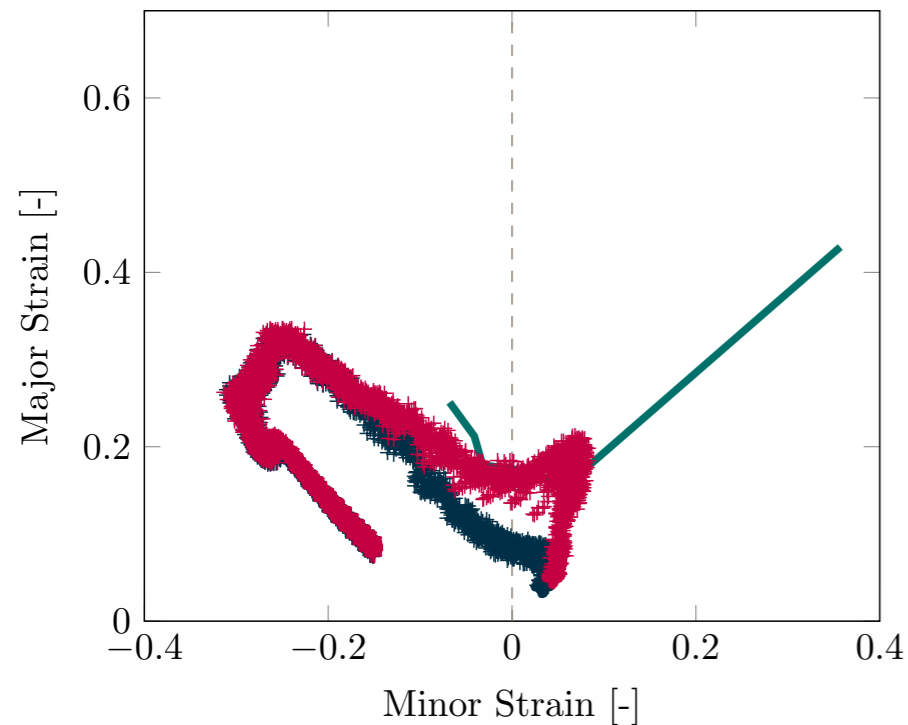
# Combined Forming



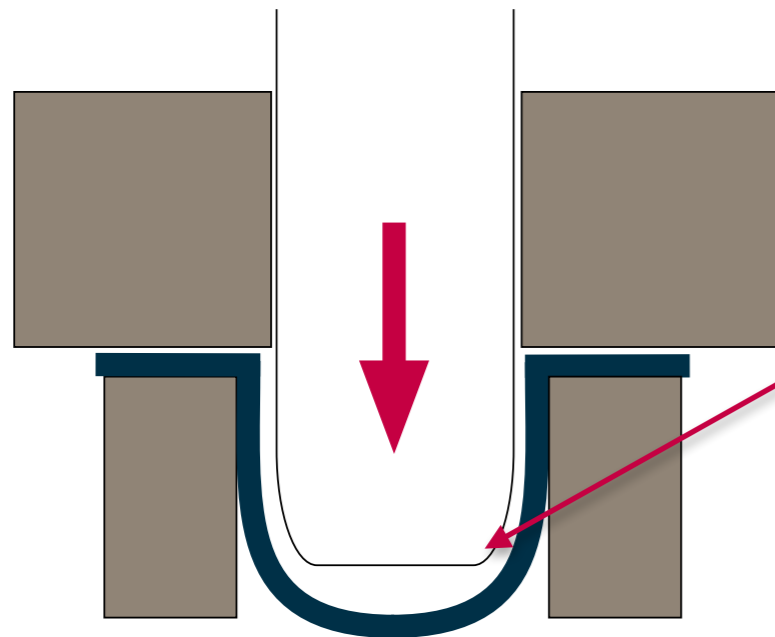
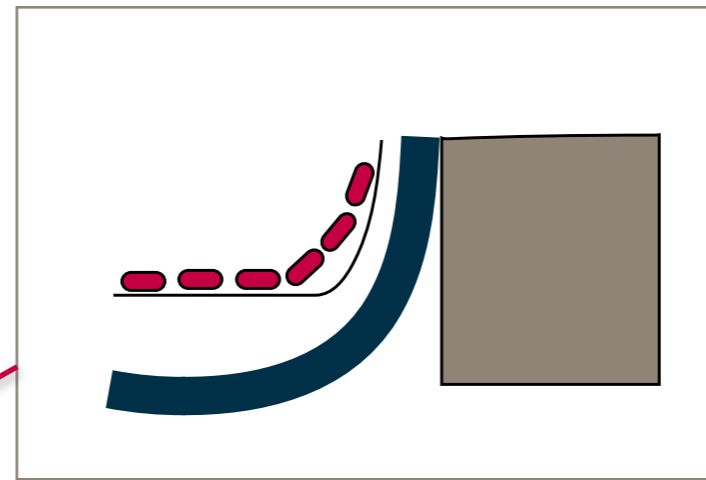
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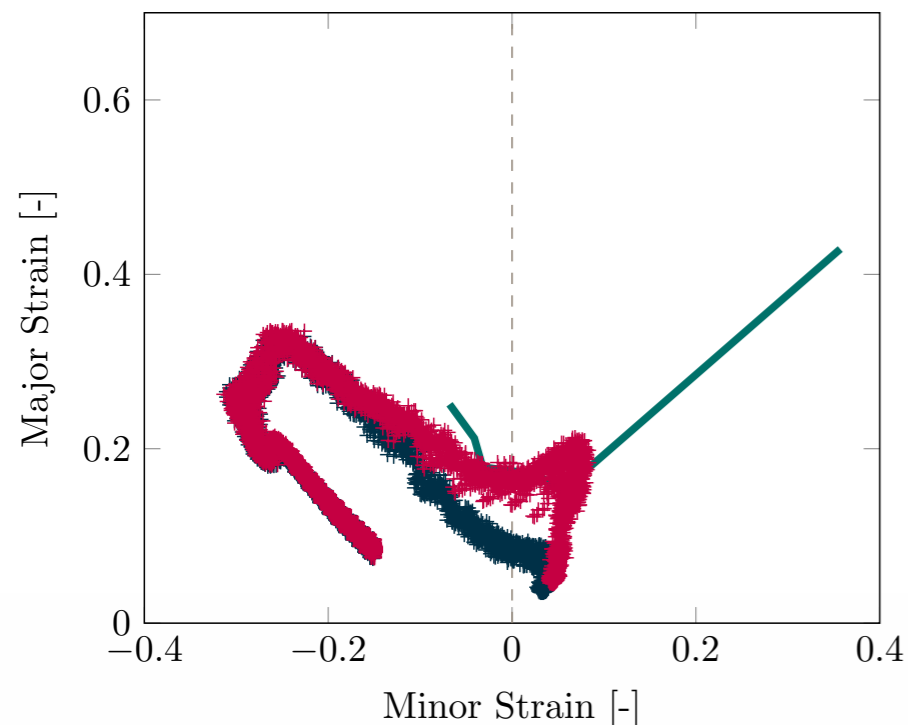
- Combination of both technologies yields forming beyond quasi static forming limits
- Reduction of wear by tool integration
- Forming of high-strength materials



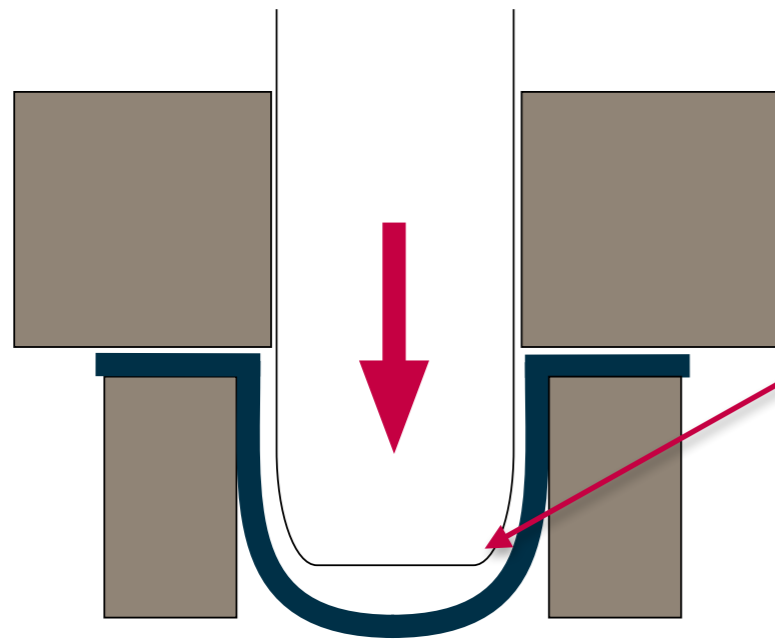
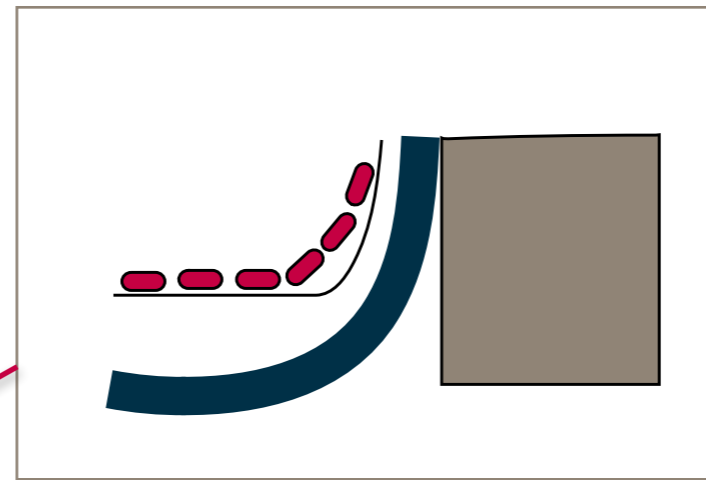
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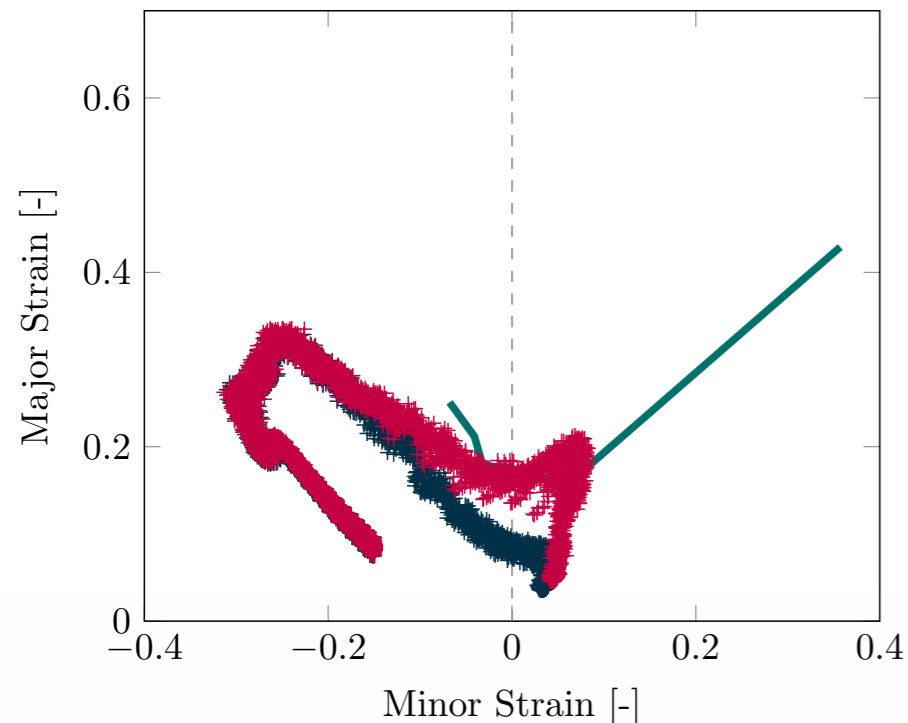
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- Forming of high-strength materials
- Process is subject to many parameters
- Only careful adjustments of involved parameters yield good results
- Economic process design necessary



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- Economic process design necessary
- ➔ Virtual process design to overcome drawbacks!

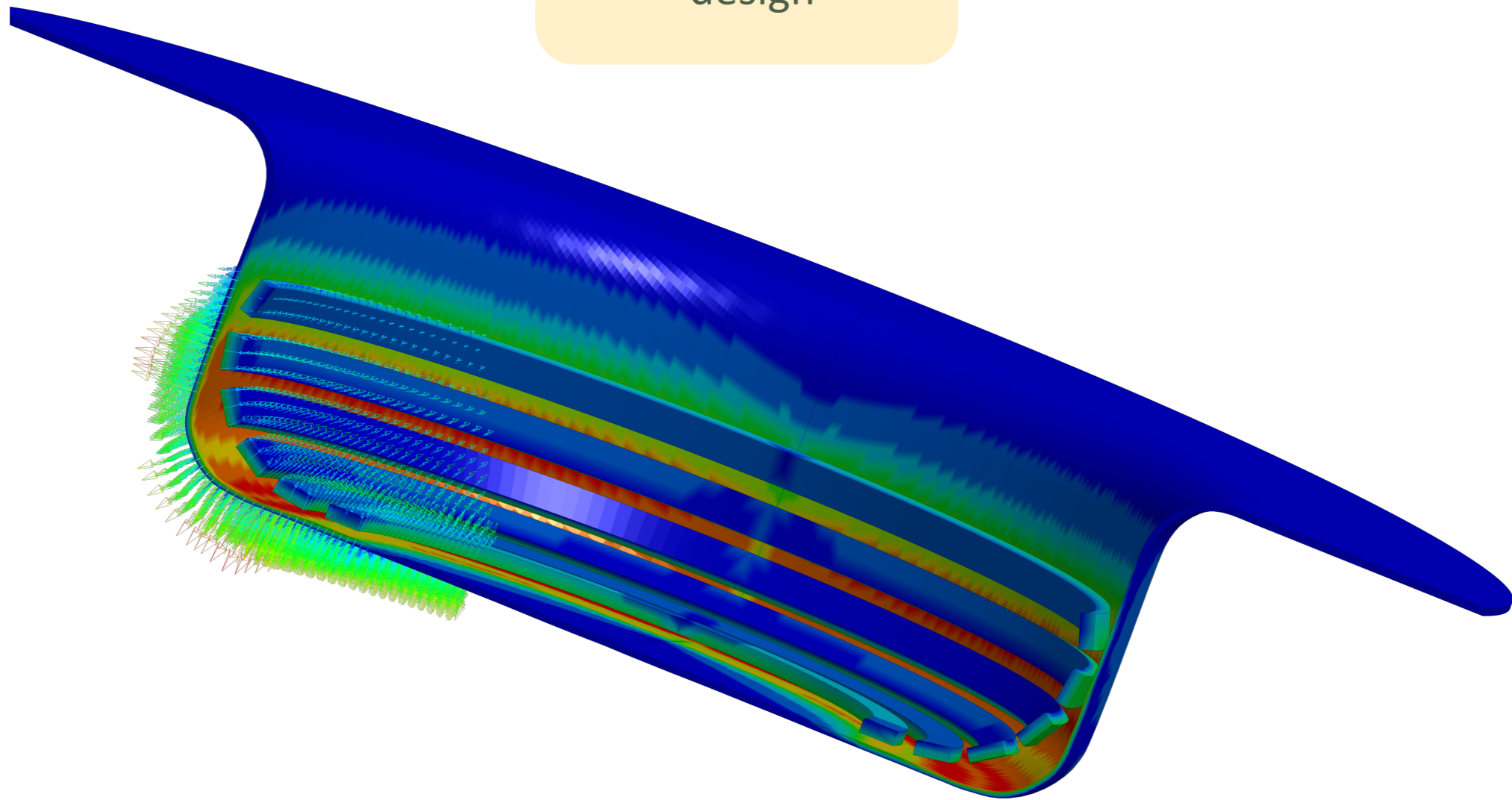


# Virtual Process Design



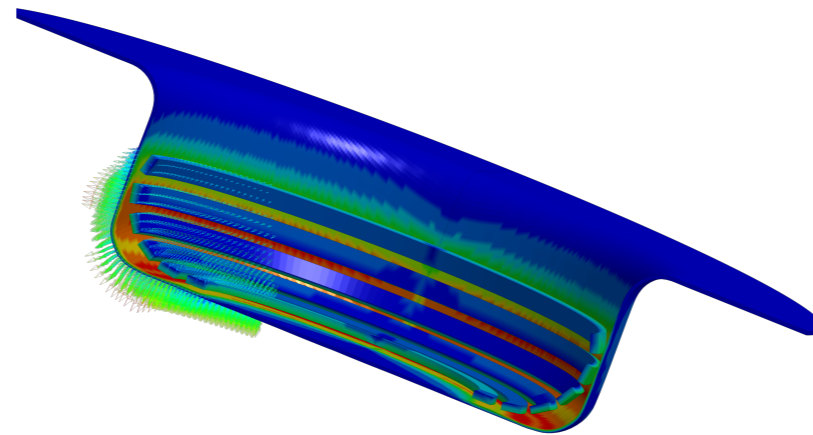
# Virtual Process Design

Enhancement by  
virtual process  
design



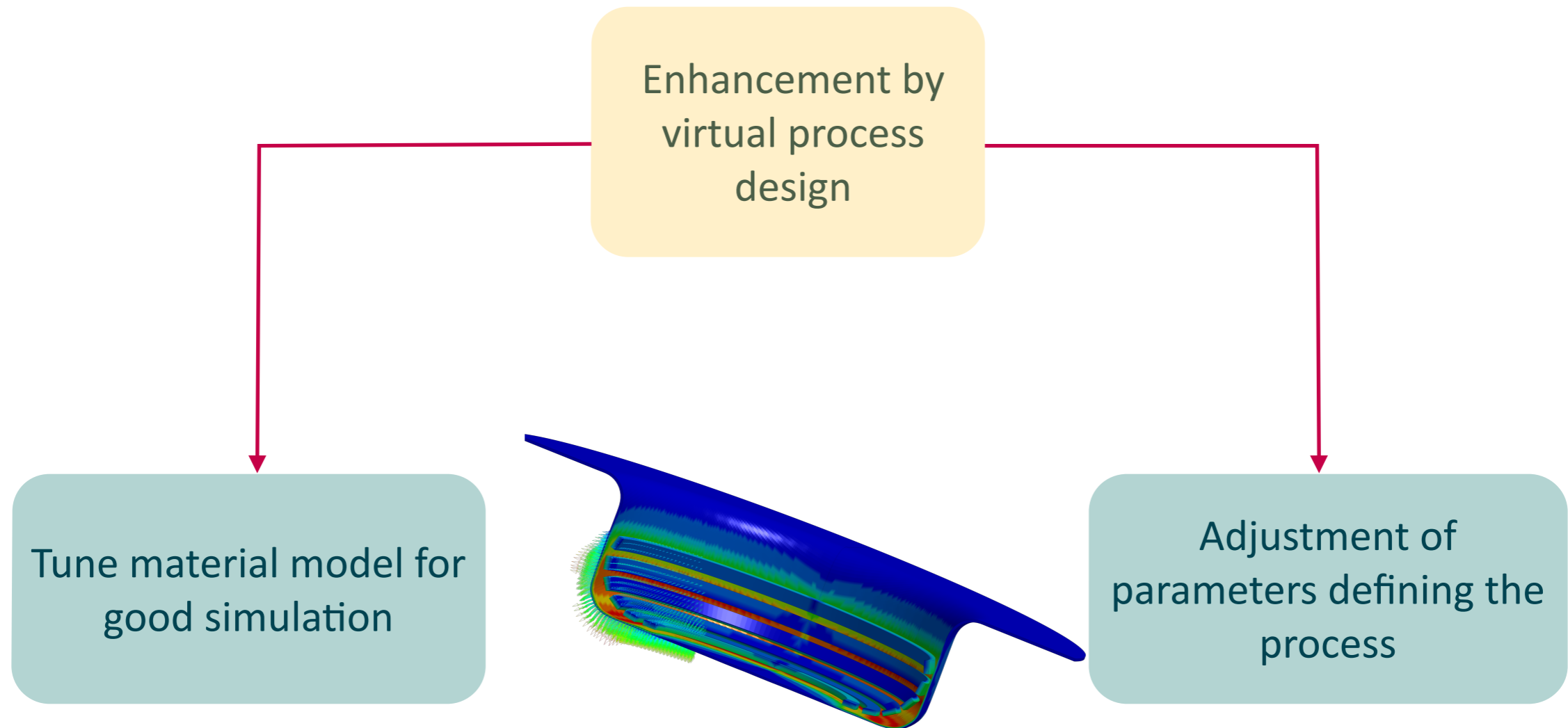
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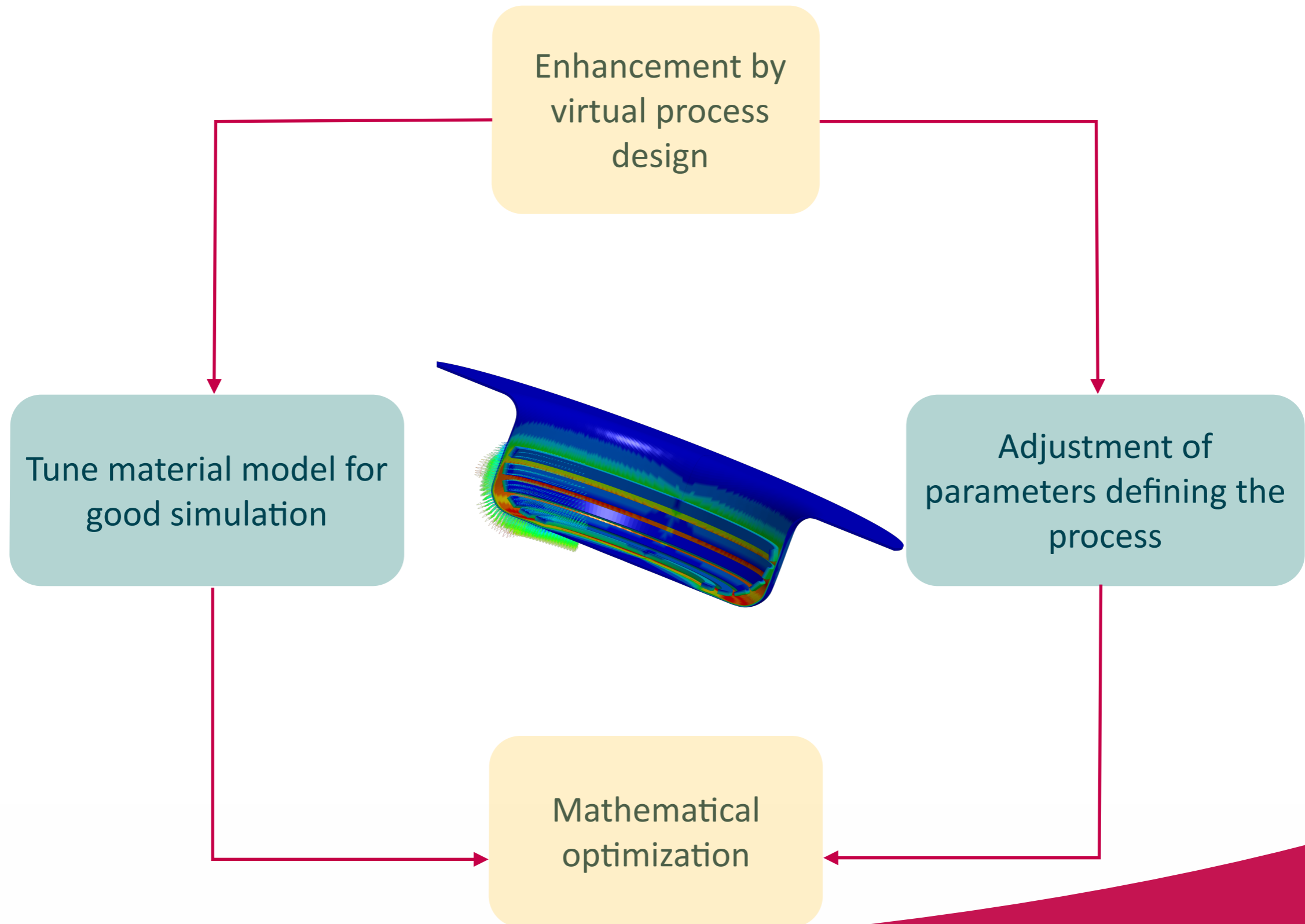


Adjustment of  
parameters defining the  
process

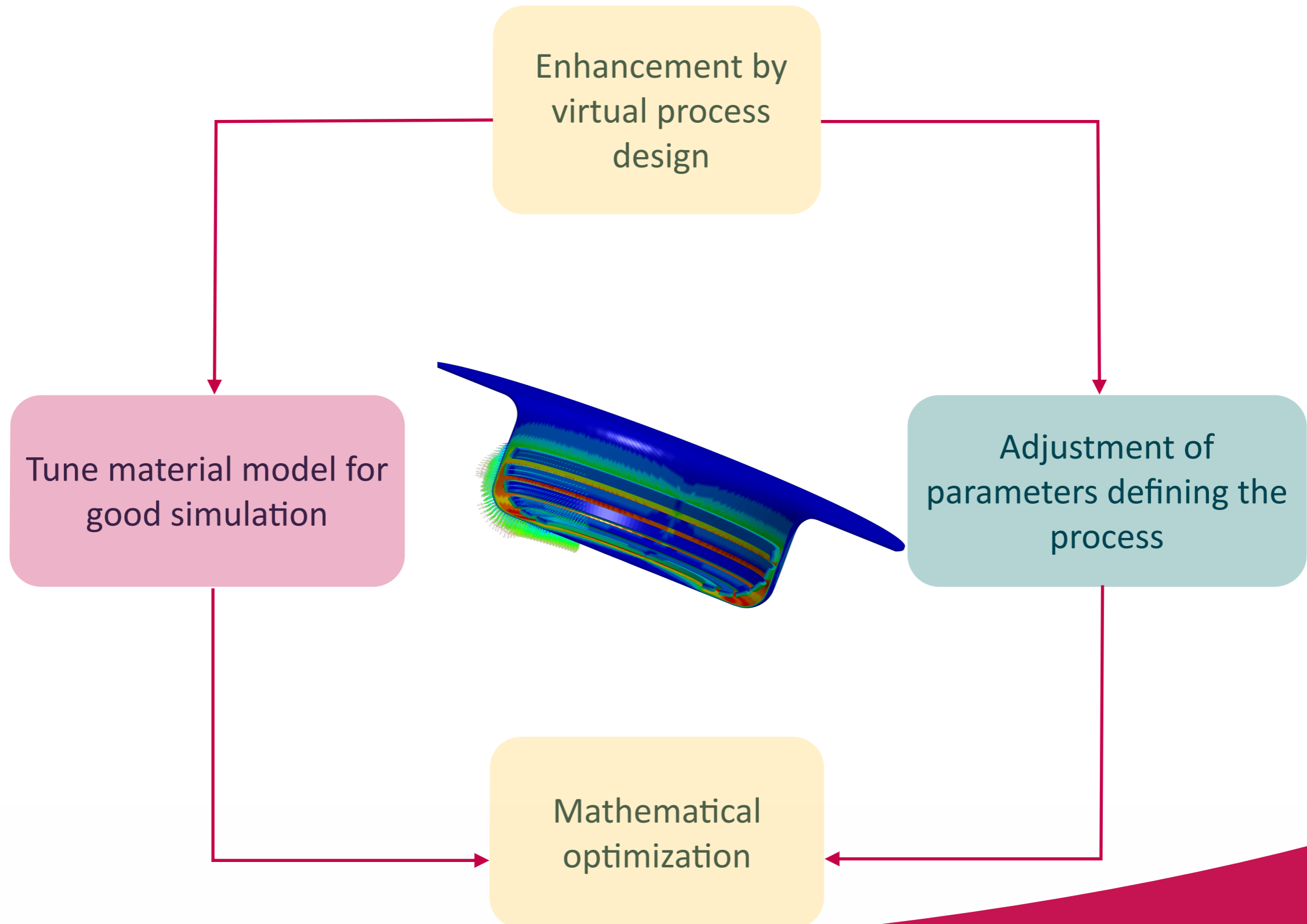
# Virtual Process Design



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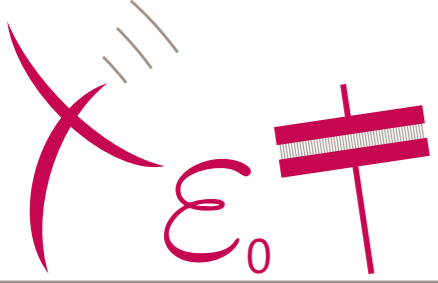
# Virtual Process Design



# Constitutive Material Model

$$S = \mu (C_p^{-1} - C^{-1}) + \frac{\lambda}{2} \left( \det C (\det C_p)^{-1} - 1 \right) C^{-1}, \quad X = c \left( C_{p_i}^{-1} - C_p^{-1} \right)$$

$$Y = CS - C_p X, \quad Y_{\text{kin}} = C_p X$$



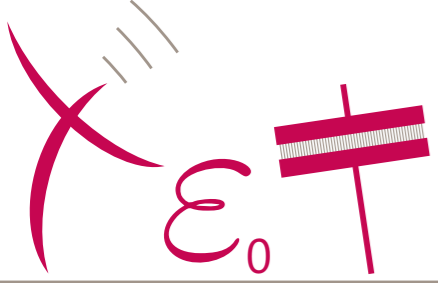
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## Ingredients:

- Equations for second order Piola-Kirchhoff stress tensor  $S$ , backstress tensor  $X$  and stress-like tensors  $Y, Y_{\text{kin}}$

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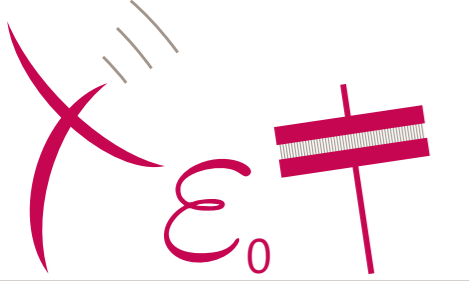
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Plastic flow rule

$$\dot{C}_p = \dot{\lambda} \frac{\text{sym} \left( C_p \left( \tilde{A} [(Y^D)^T] + (\tilde{A}^T [Y^D])^T \right)^D \right)}{\sqrt{Y^D \cdot (\tilde{A} [(Y^D)^T])}}$$





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Kinematic hardening

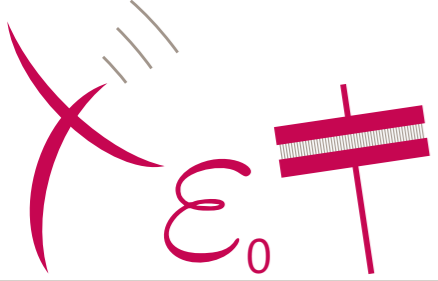
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Isotropic hardening

$$\dot{\kappa} = \sqrt{\frac{2}{3}} \dot{\Lambda}$$

Kinematic hardening

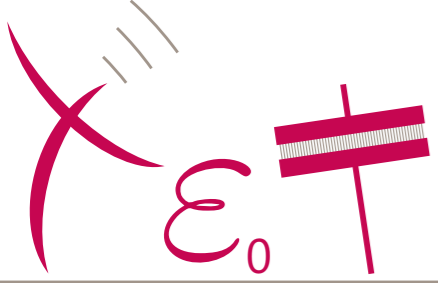
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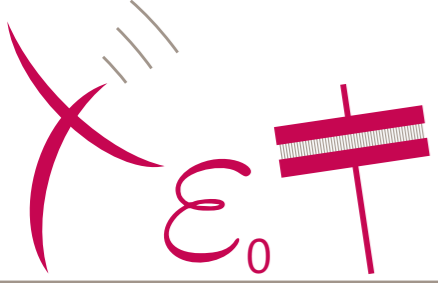


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- Yield function of Hill-type

$$\Phi = \sqrt{Y^D \cdot \left( \tilde{A} \left[ (Y^D)^T \right] \right)} - \sqrt{\frac{2}{3}} \left( \sigma_y + Q \left( 1 - e^{-\beta \kappa} \right) \right)$$



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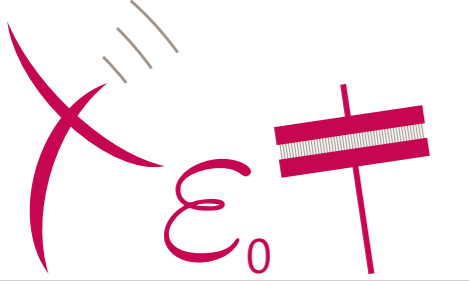
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High-speed part

$$\dot{\Lambda} = \frac{\langle \Phi \rangle^m}{\eta}$$



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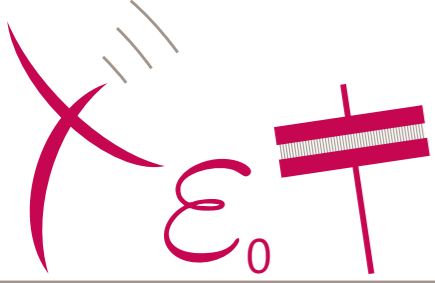
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Quasi-static part

$$\dot{\lambda} \geq 0, \quad \Phi \leq 0, \quad \dot{\lambda} \Phi = 0$$

High-speed part

$$\dot{\lambda} = \frac{\langle \Phi \rangle^m}{\eta}$$

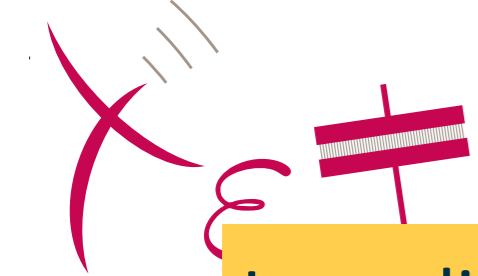


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- Scalar damage variable (Lamaitre type)

$$\dot{D} = \dot{\lambda} \sqrt{\frac{2}{3}} \frac{1}{1-D} \left( \frac{Y_0}{s} \right)^k H(\kappa - p_D)$$



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- Scalar damage variable (Lamaitre type)
- Effective stress contributions

$$\bar{S} = \frac{1}{1 - D} S, \quad Y = C\bar{S} - C_p X$$

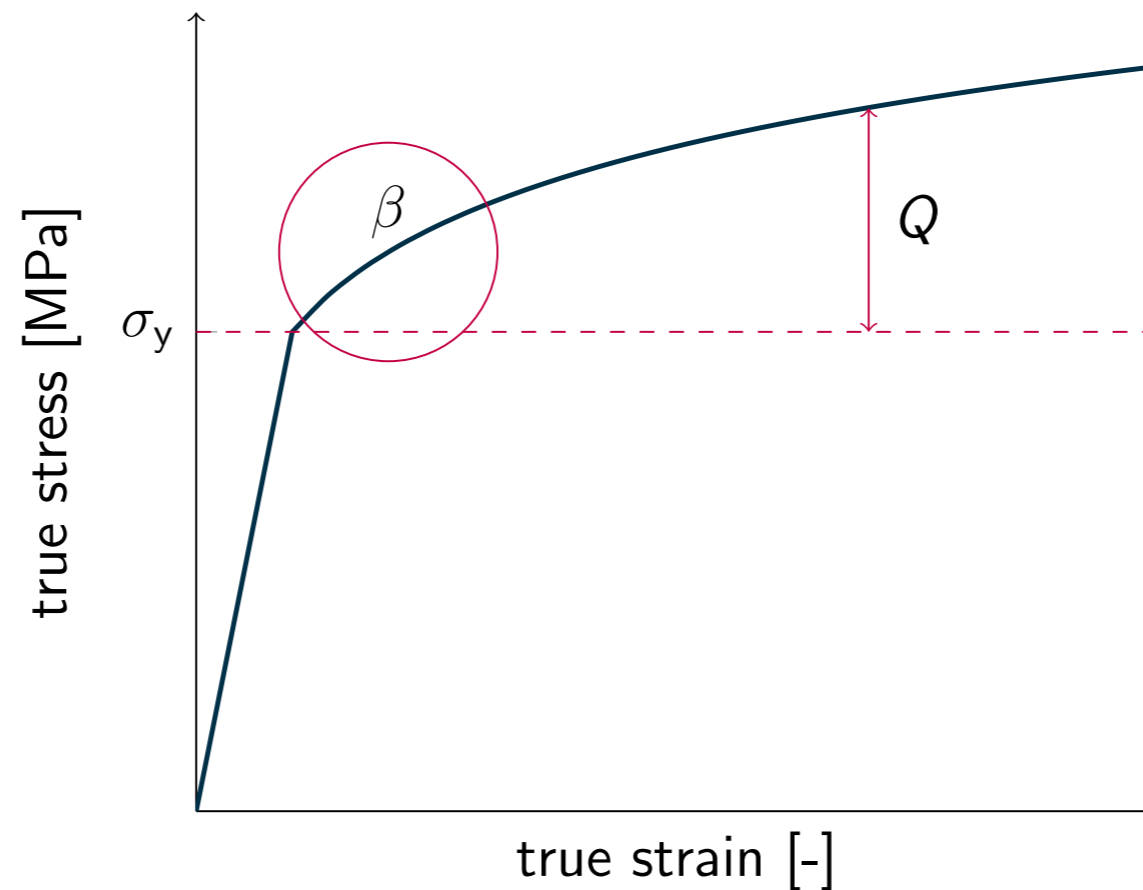
- Isotropic hardening parameters in the yield function

$$\Phi = \sqrt{Y^D \cdot \left( \tilde{\mathcal{A}} \left[ (Y^D)^T \right] \right)} - \sqrt{\frac{2}{3}} \left( \sigma_y + Q \left( 1 - e^{-\beta \kappa} \right) \right)$$



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$$\dot{C}_{p_i} = 2\dot{\Lambda} \frac{b}{c} Y_{\text{kin}}^D C_{p_i}$$

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# Parameter of the Constitutive Material Model

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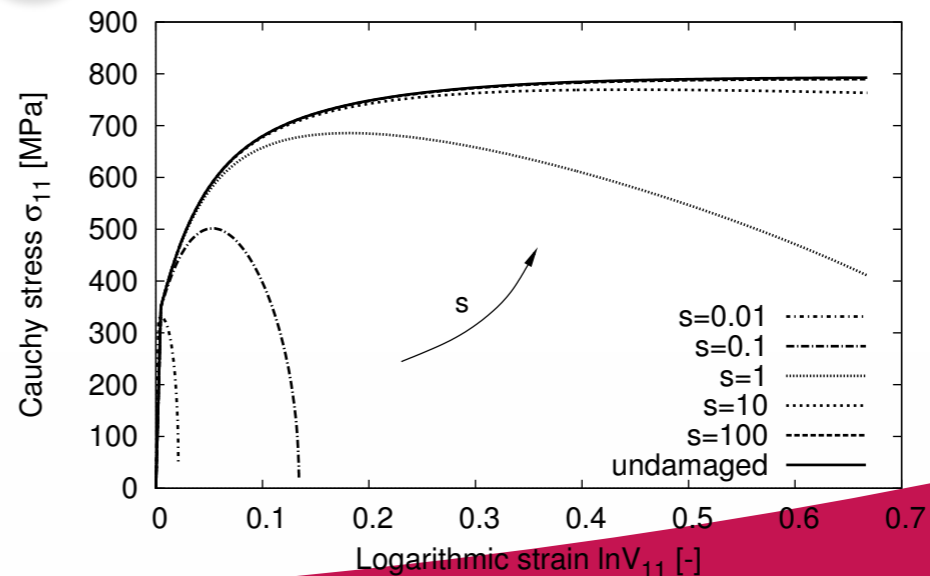
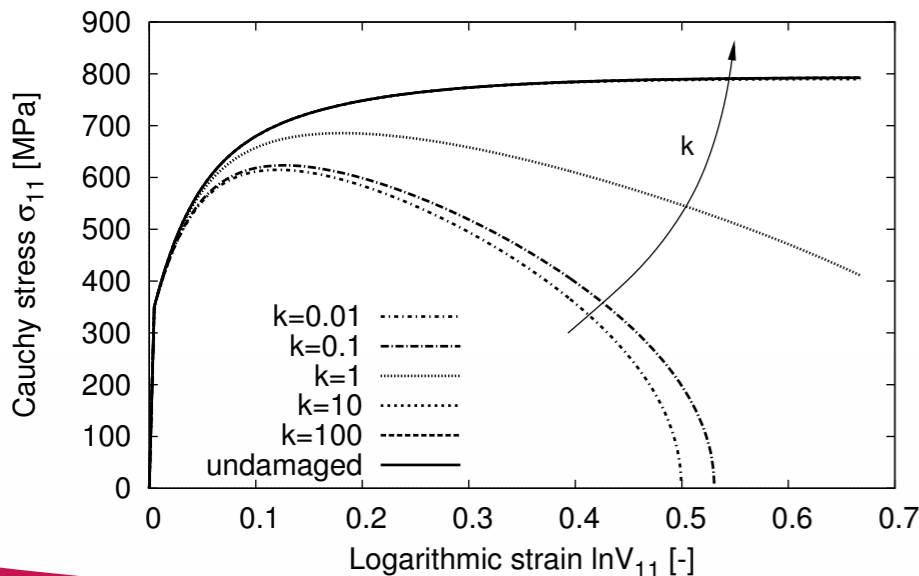
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Flow curves - dependence on k (s=1, pd=0)

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- Challenge: Also identify the elastic modulus  $E$  of the material under consideration

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→ End up with a total of 9 parameters to be identified

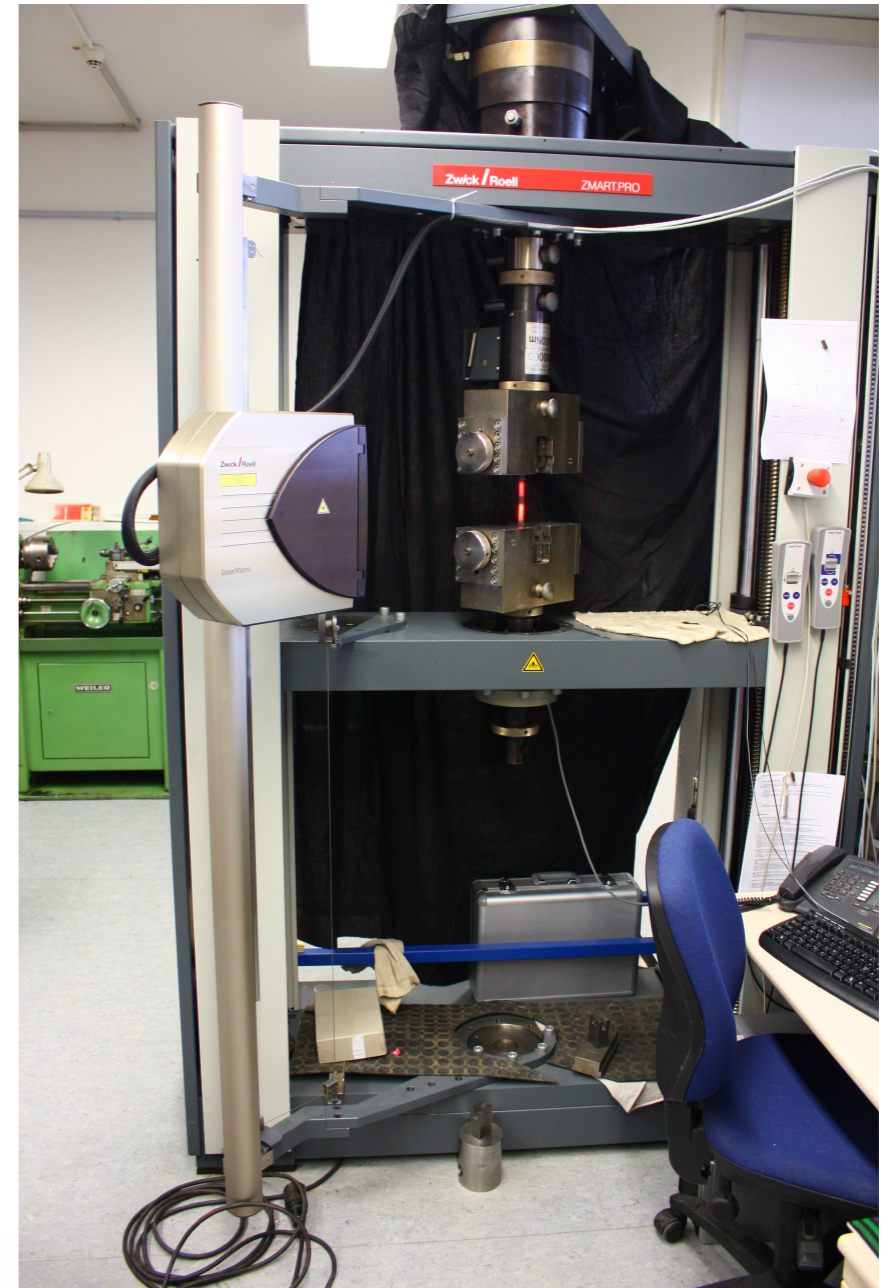
# Identification by Non-Linear Optimization

- Parameters are identified by fitting the model to experimental force-displacement curves

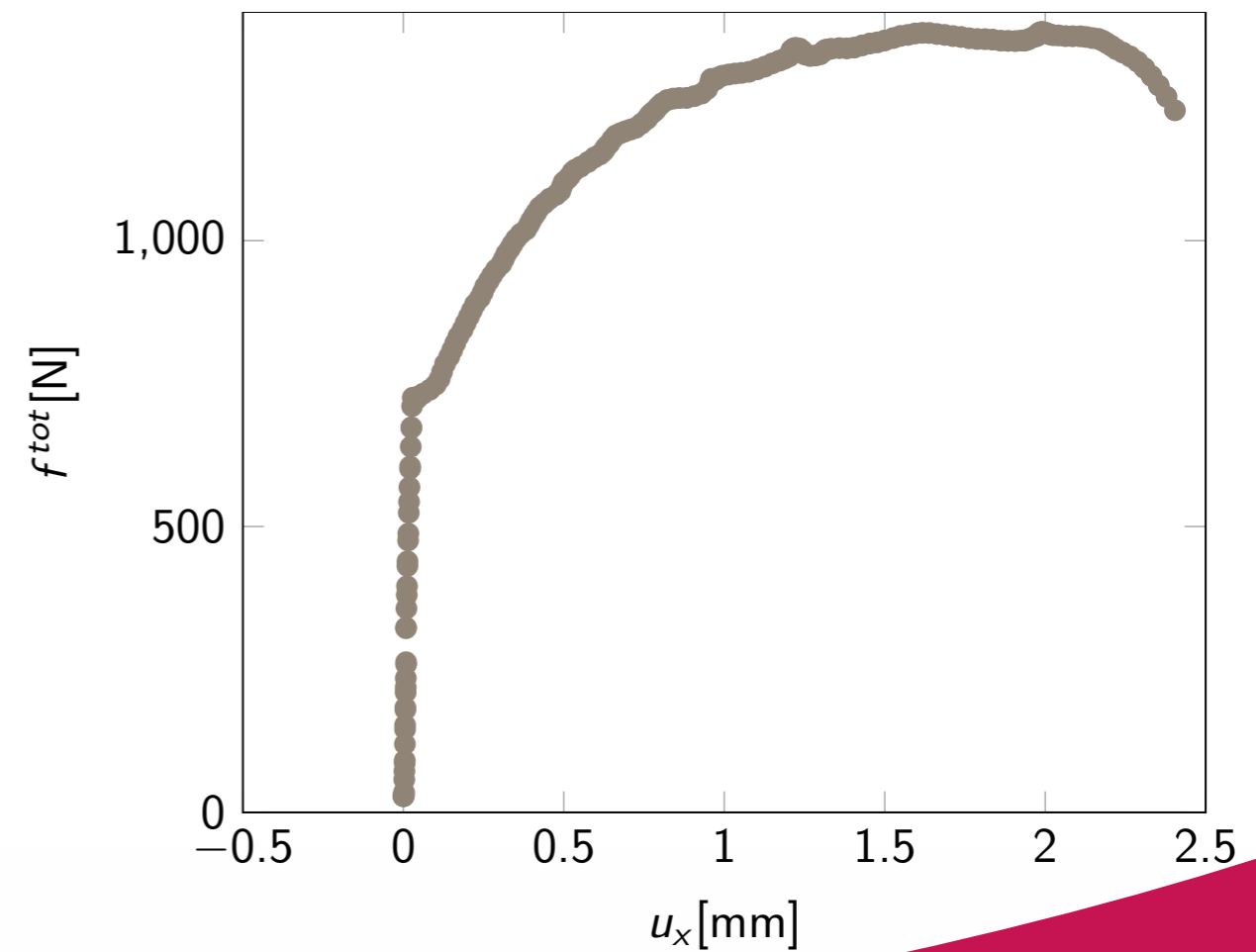
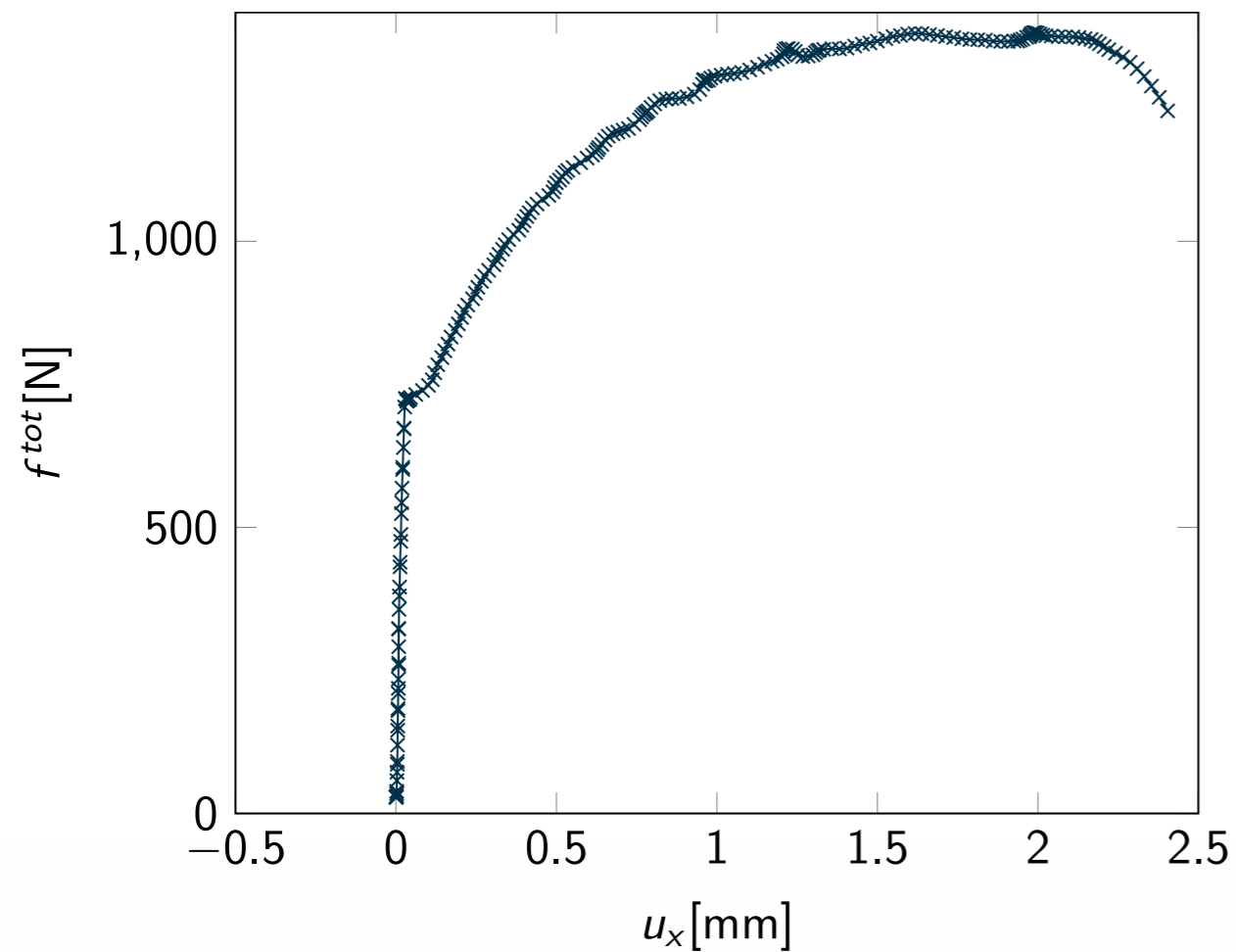
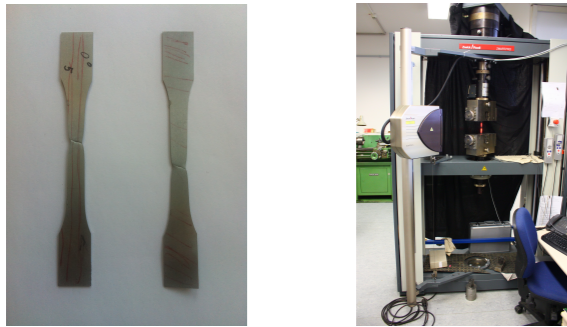


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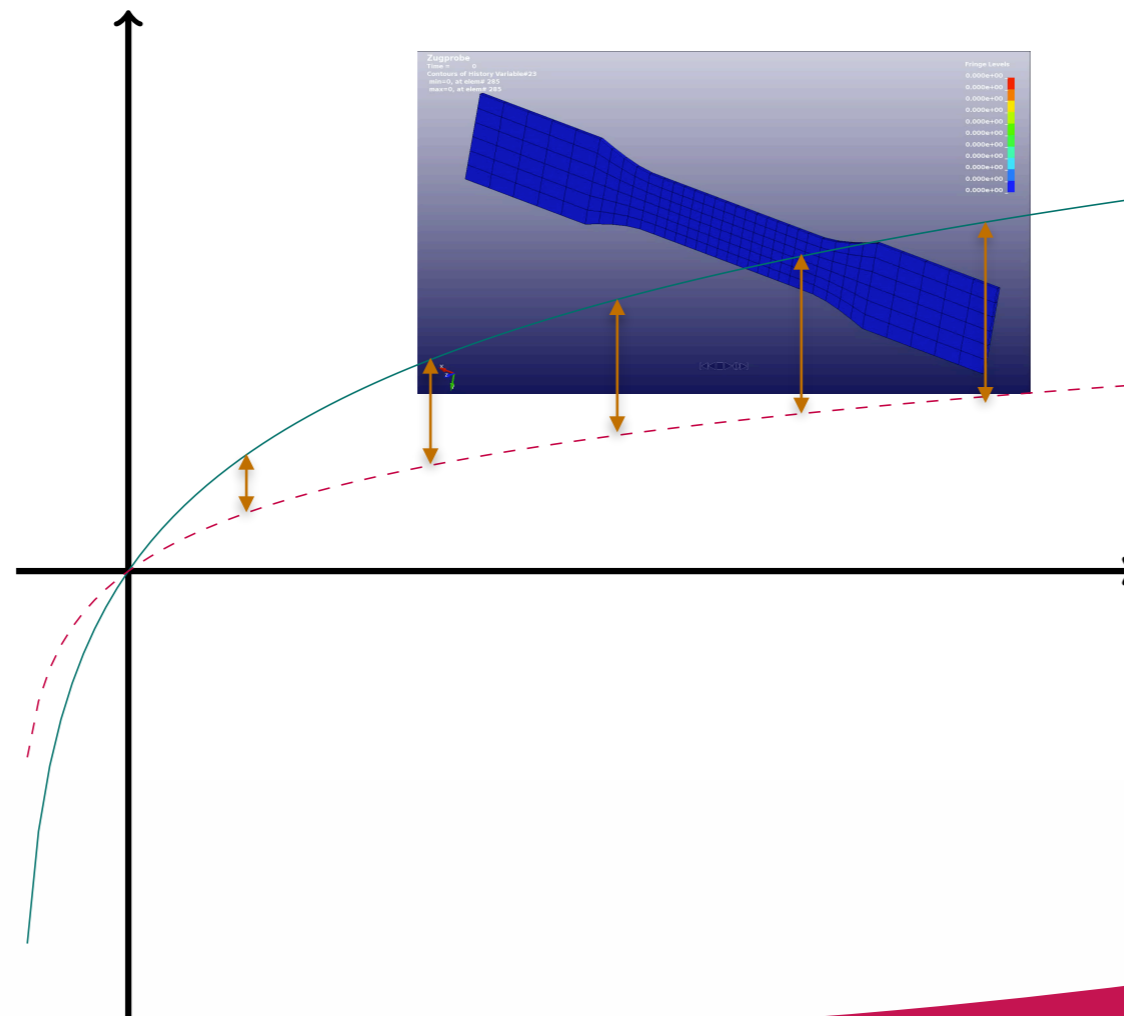
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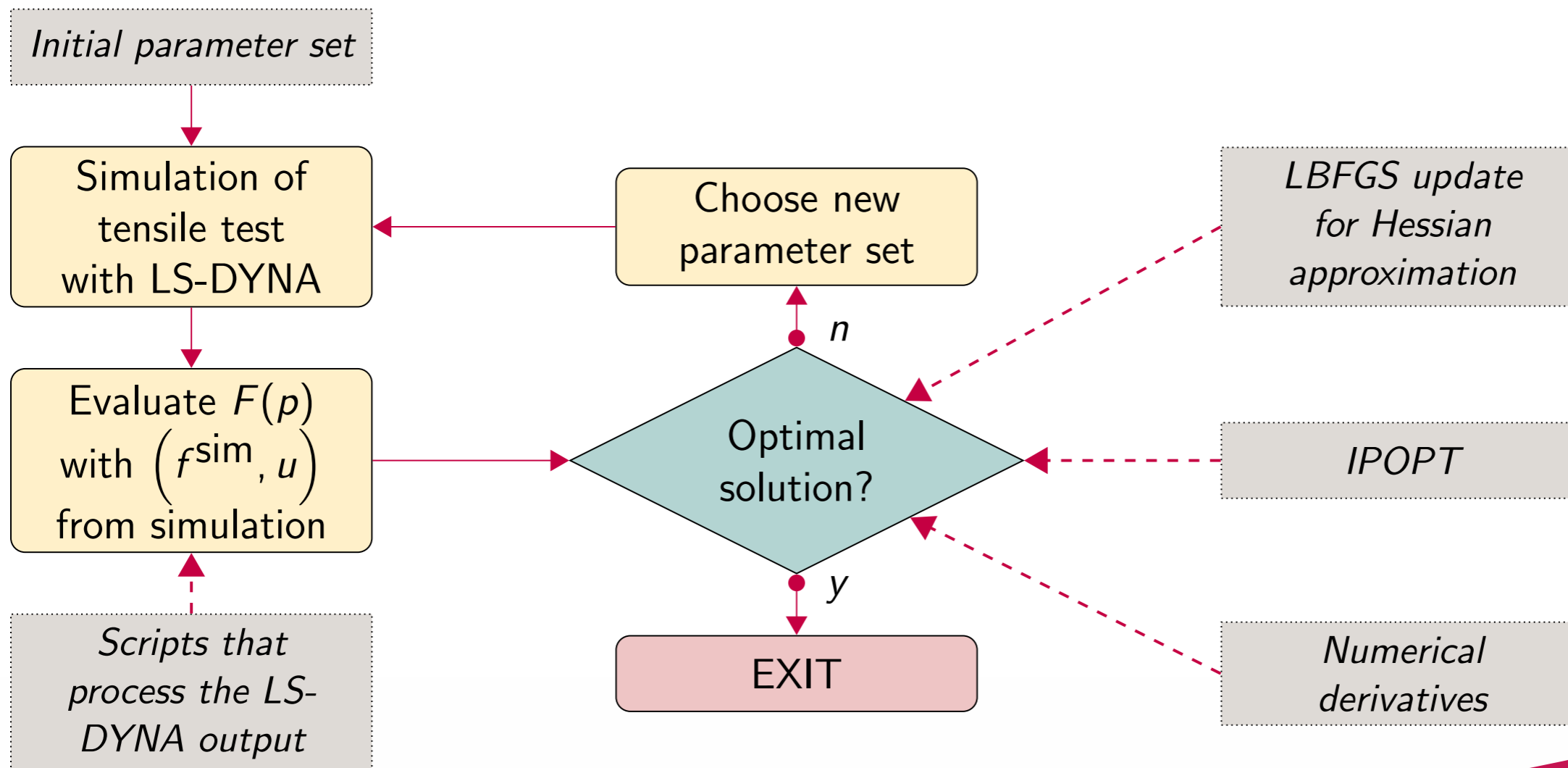
- Parameters are identified by fitting the model to experimental force-displacement curves
- Non-linear objective function to identify optimal parameter vector  $p$

$$F(p) = \frac{1}{2(u_N - u_1)} \sum_{i=1}^{N-1} (u_{i+1} - u_i) \left[ (f_{i+1}^{\text{sim}}(p) - f_{i+1}^{\text{exp}})^2 + (f_i^{\text{sim}}(p) - f_i^{\text{exp}})^2 \right]$$

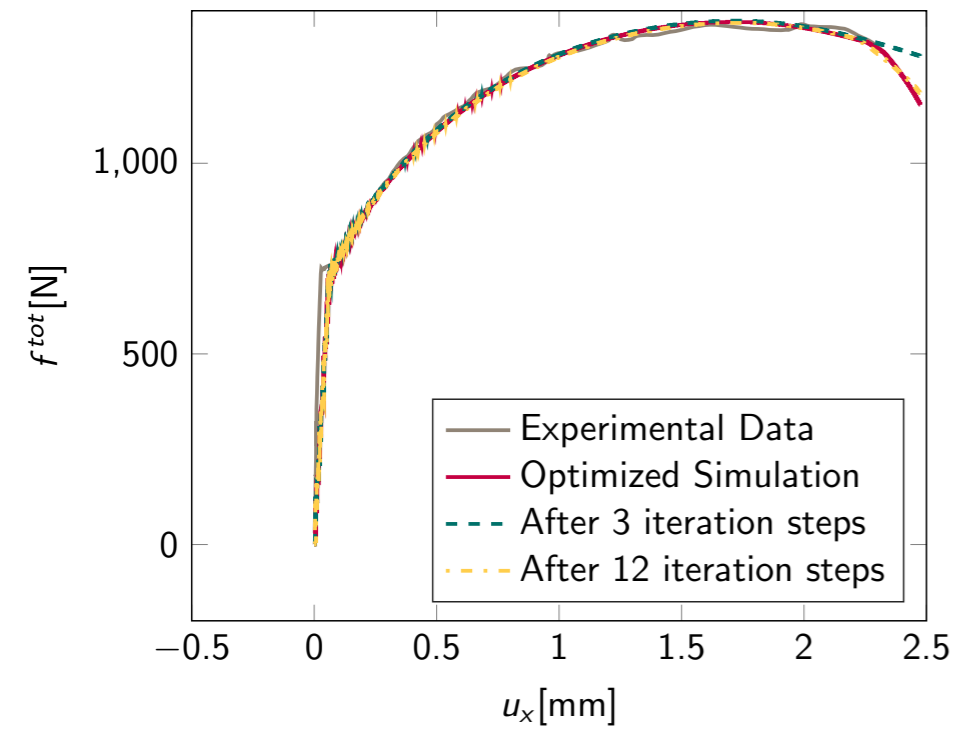


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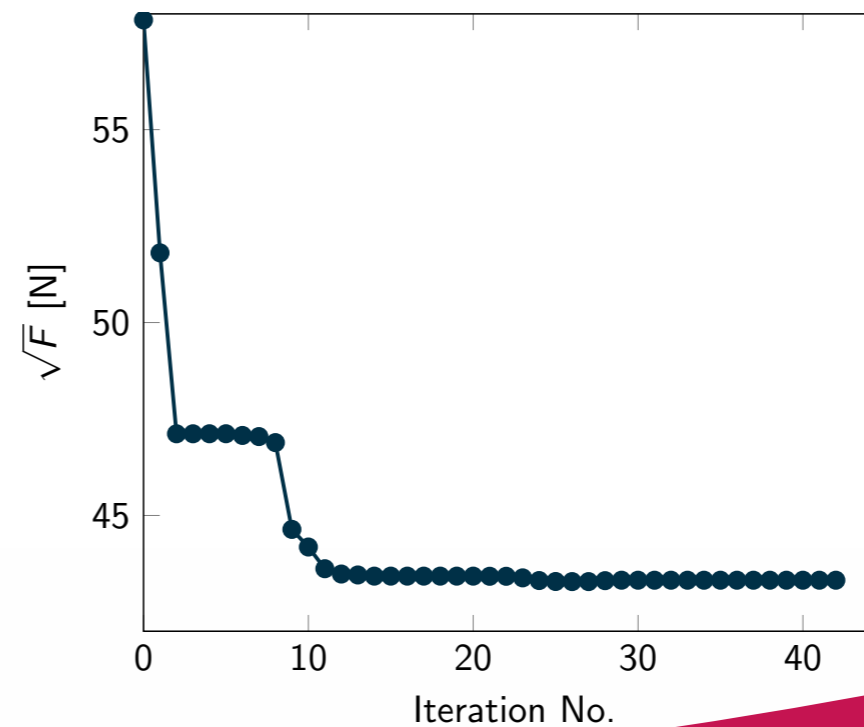
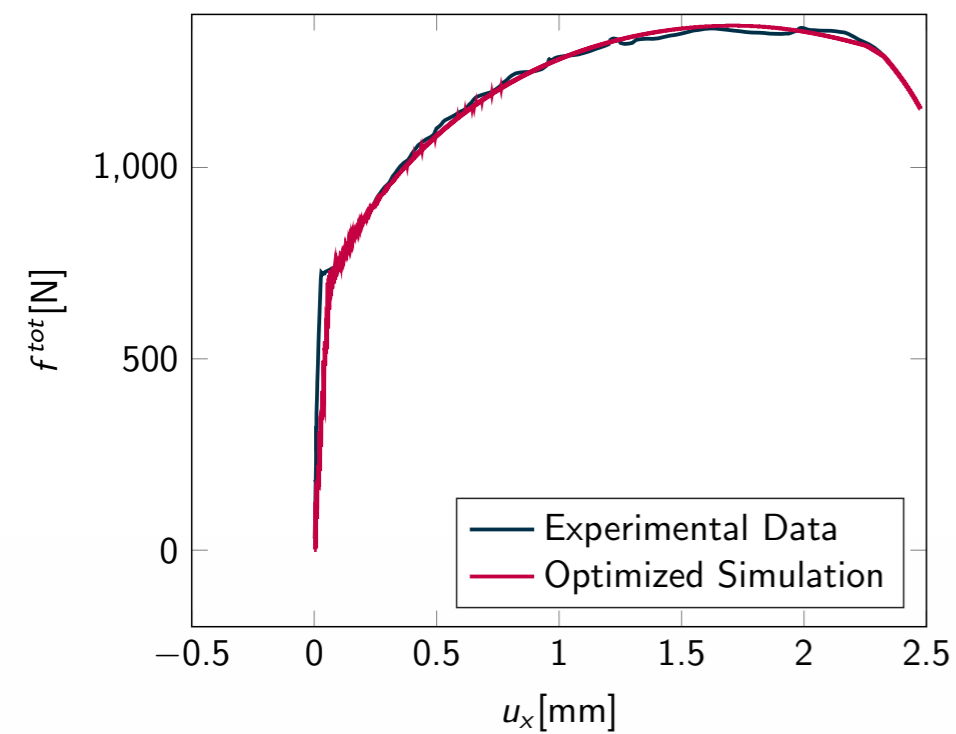
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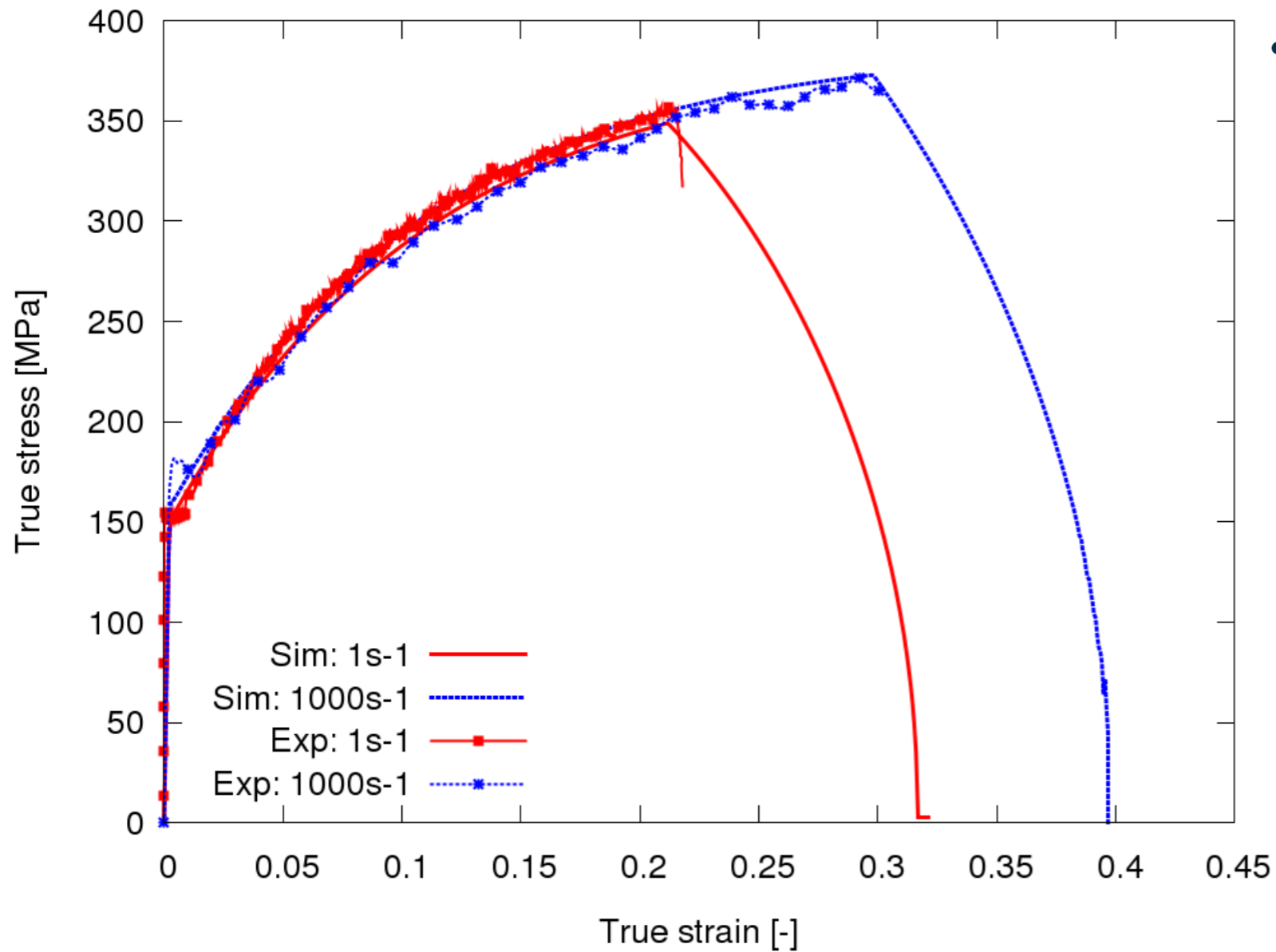
# Identification by Non-Linear Optimization



Parameter	Identified value
$Q$	$1.604 \cdot 10^2$
$\beta$	$1.265 \cdot 10^1$
$k$	$4.694 \cdot 10^{-1}$
$s$	$2.680 \cdot 10^{-1}$
$\rho_D$	$6.306 \cdot 10^{-1}$
$E$	$8.089 \cdot 10^4$
$\sigma_y$	$1.185 \cdot 10^2$
$b$	$5.124 \cdot 10^{-3}$
$c$	$4.598 \cdot 10^{-4}$



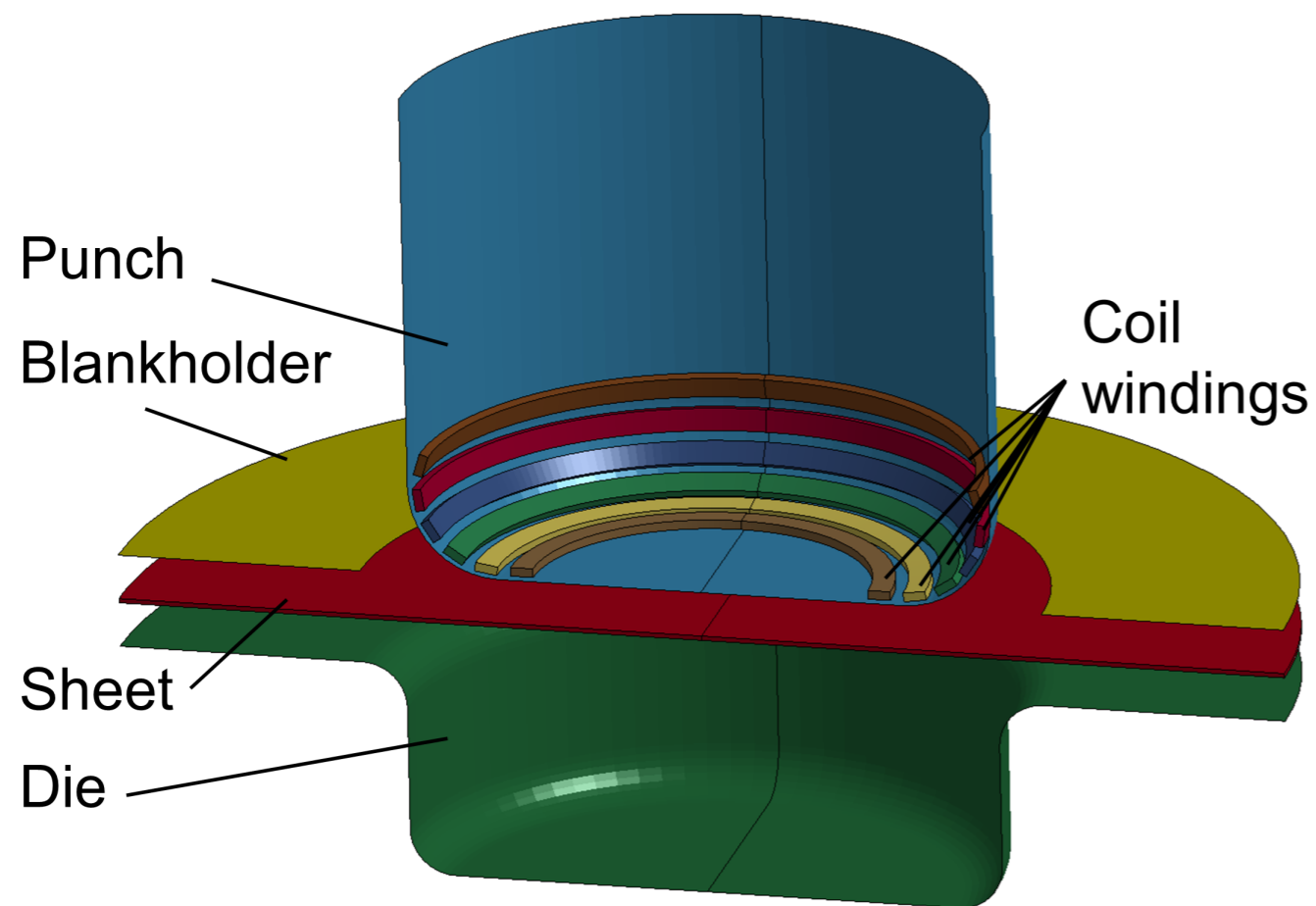
# Validation and Verification



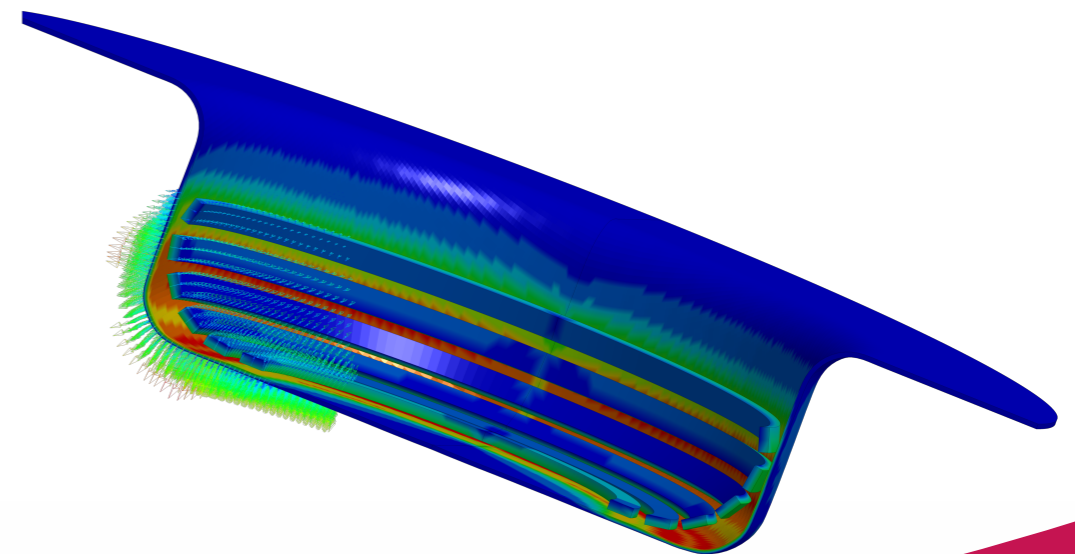
- Comparison to stress-strain curves (with evolution model for damage threshold)



# Validation and Verification



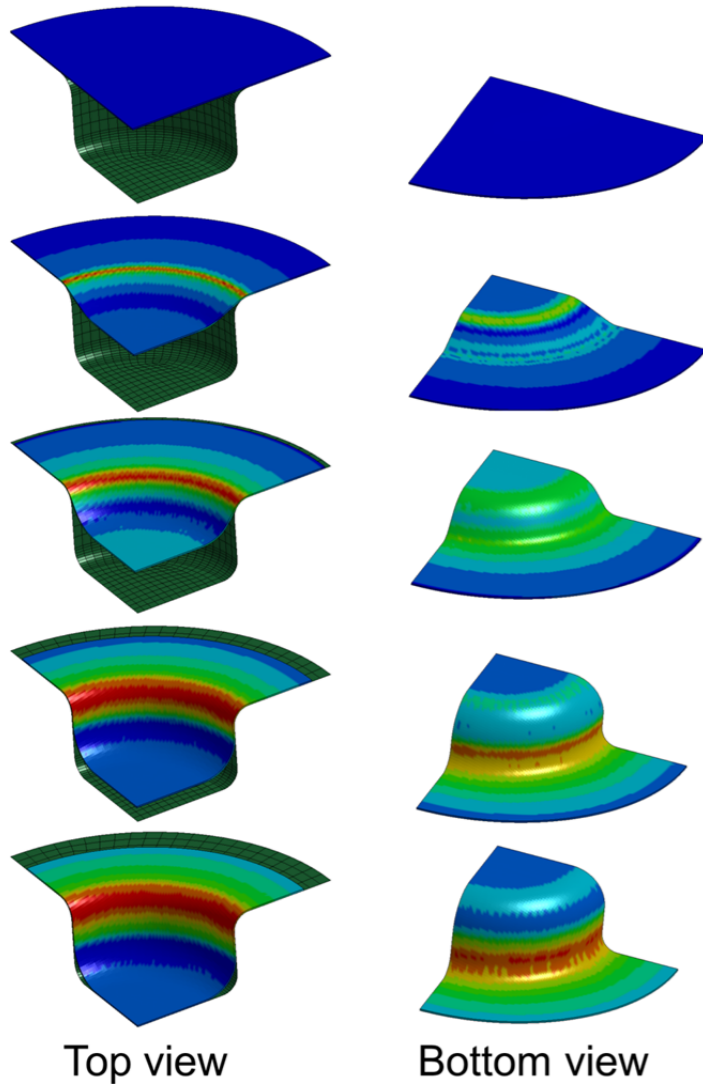
- Comparison to stress-strain curves (with evolution model for damage threshold)
- Application to complex situation (cup drawing)



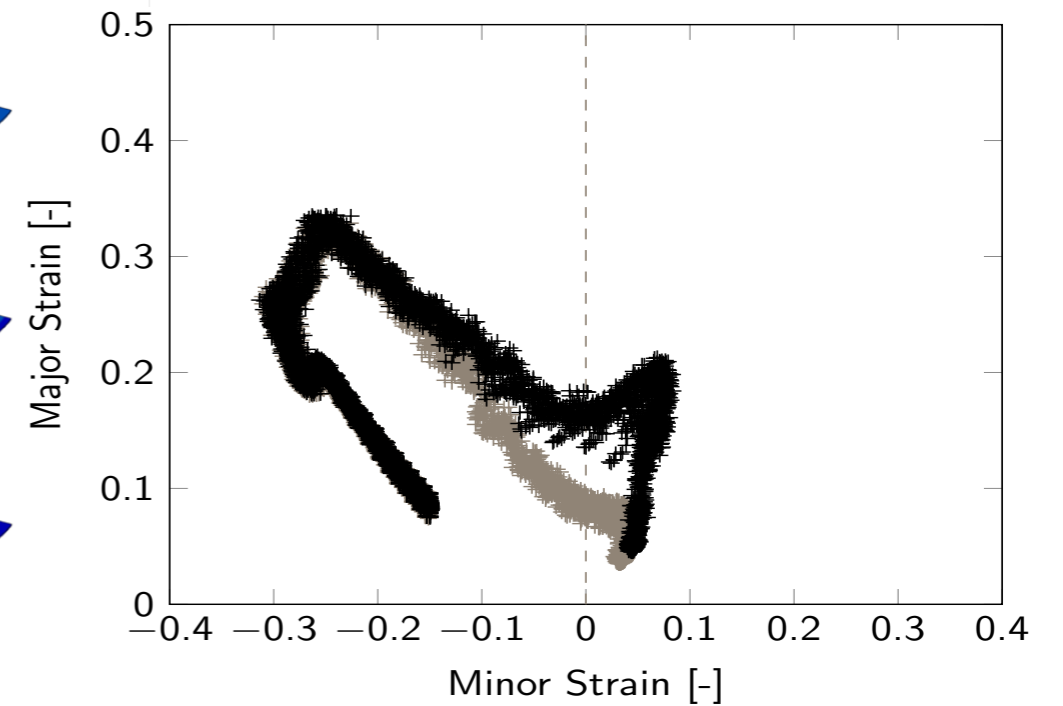
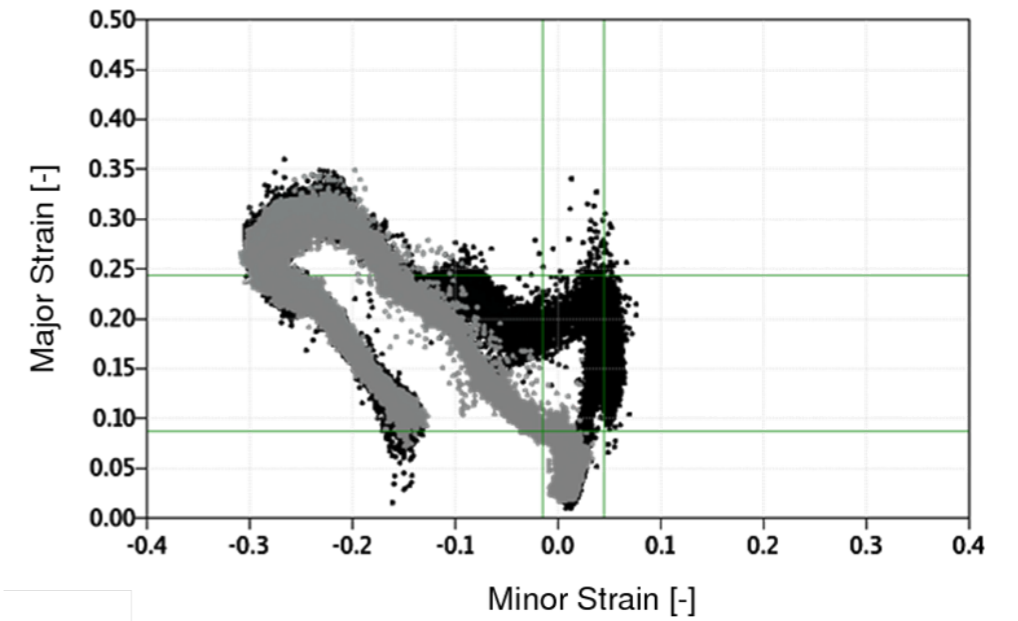
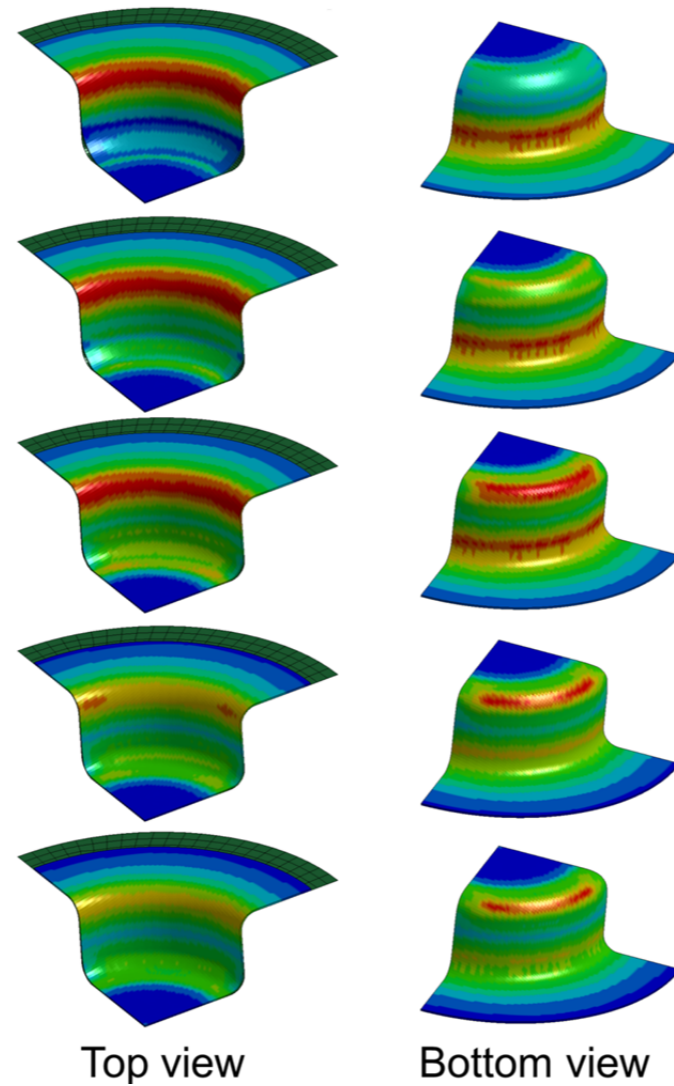
# Combined Deep Drawing of a Cup

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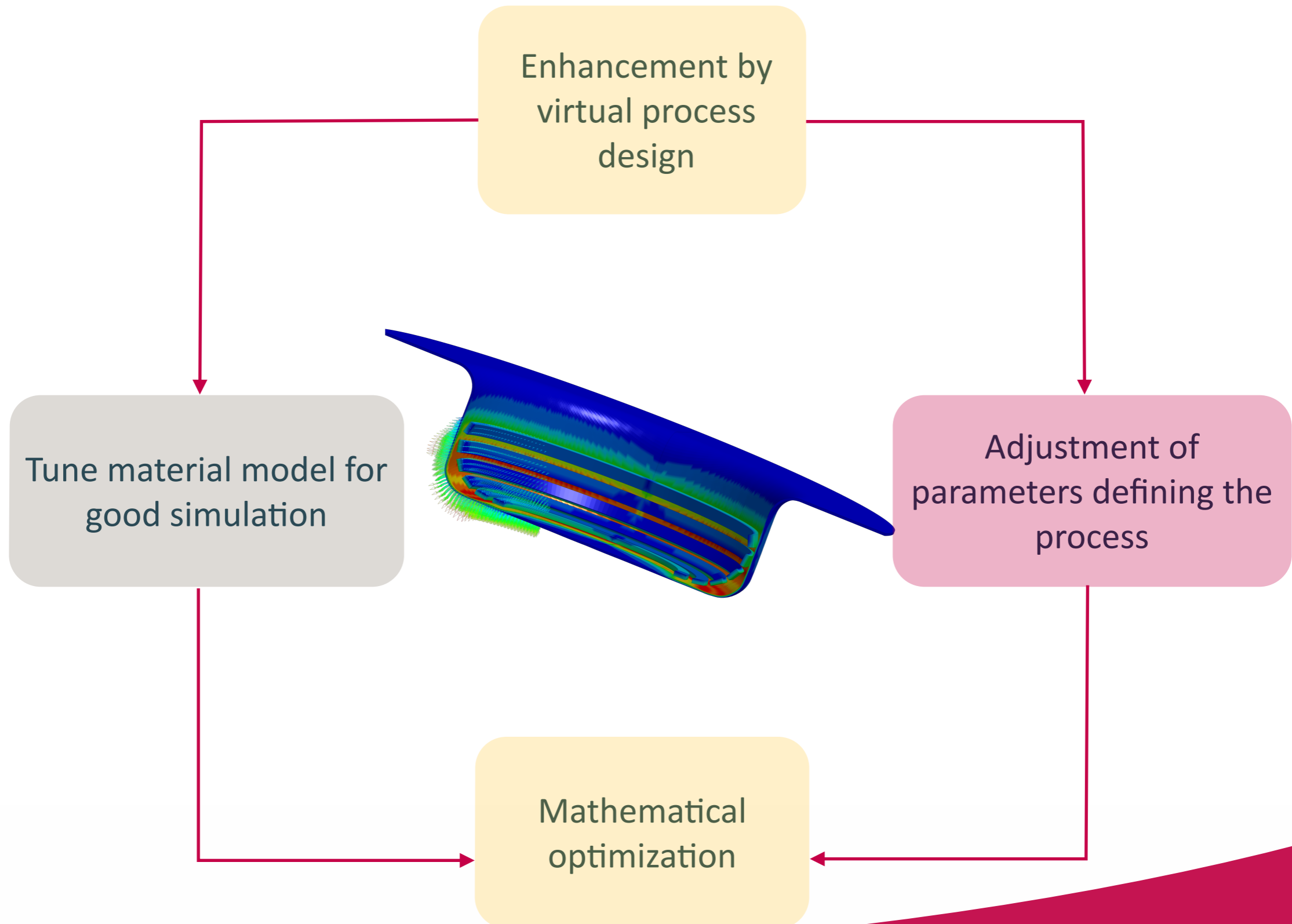
Deep drawing



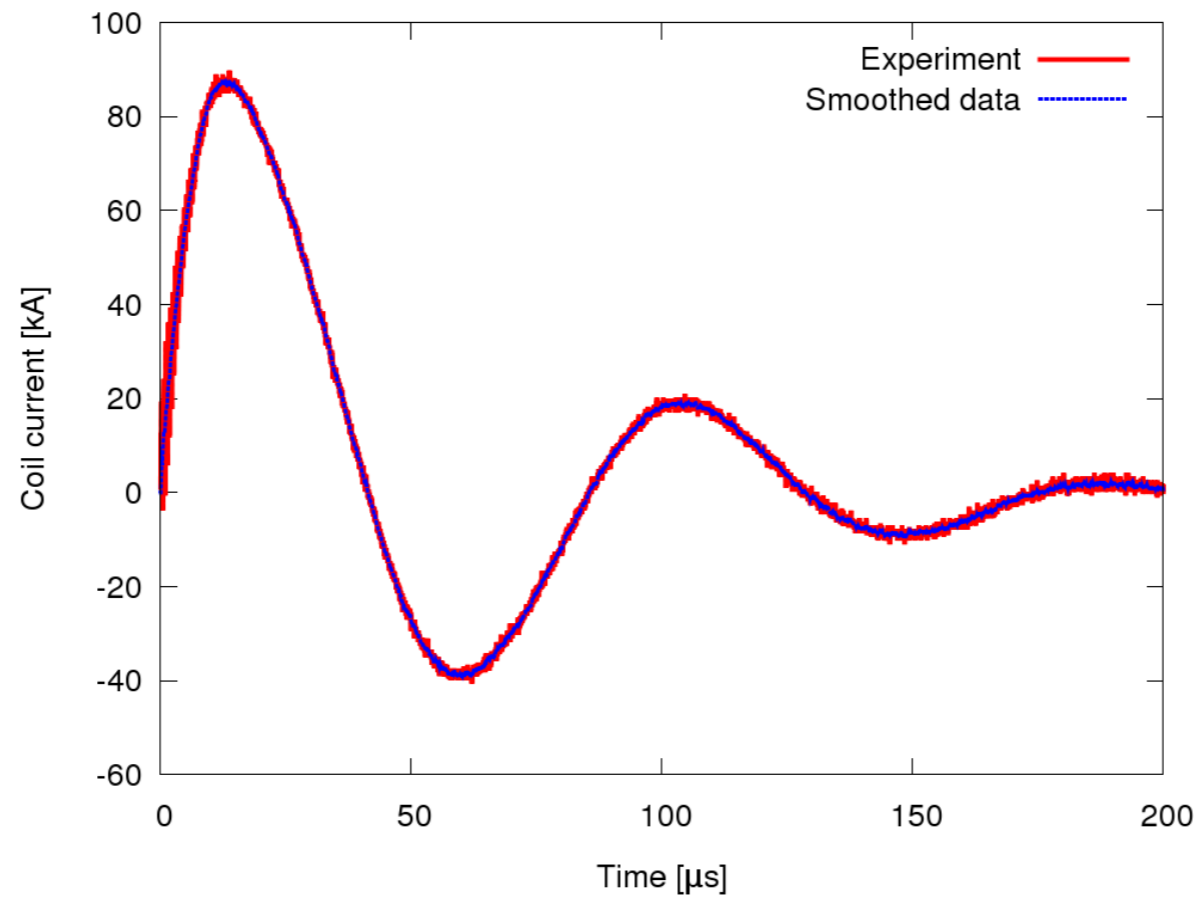
Electromagnetic forming



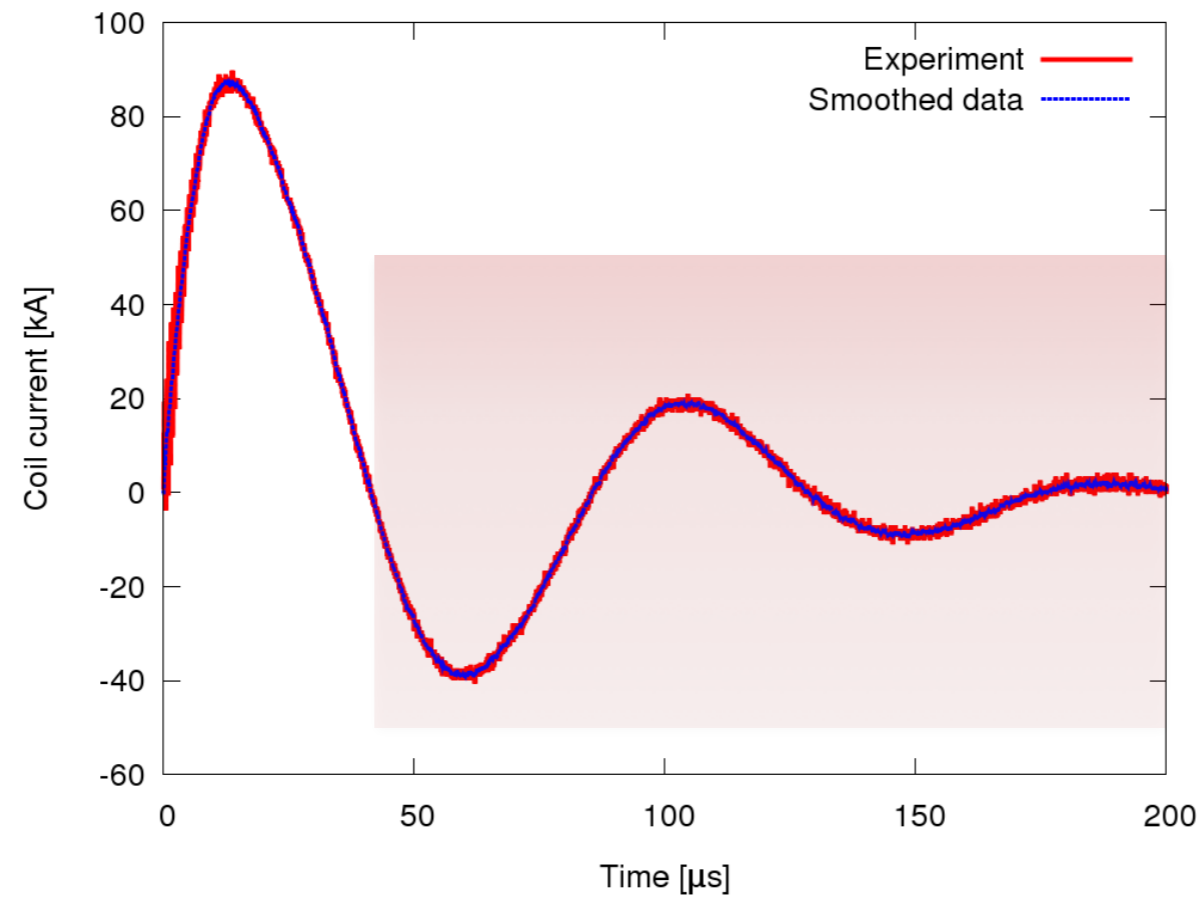
# Virtual Process Design



# Process Optimization in Cup Forming

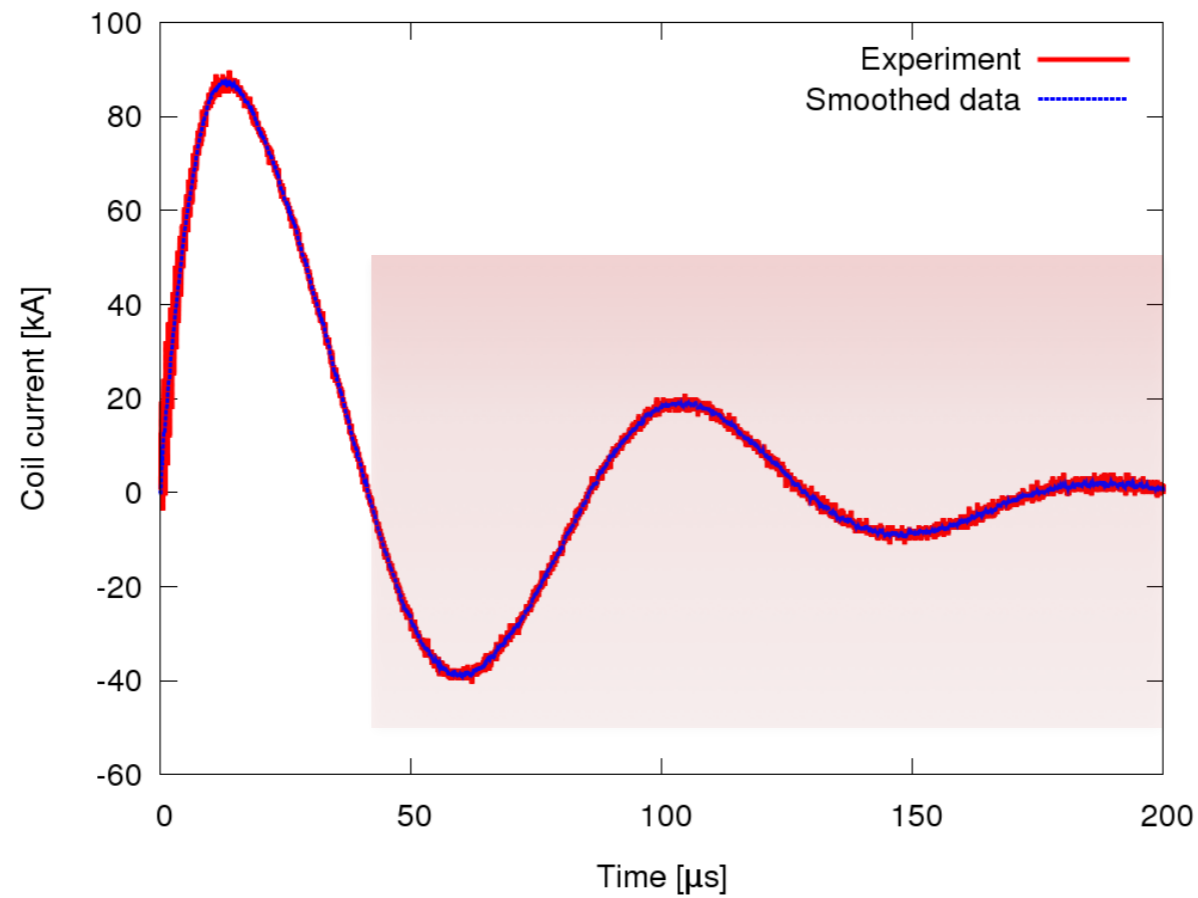


# Process Optimization in Cup Forming

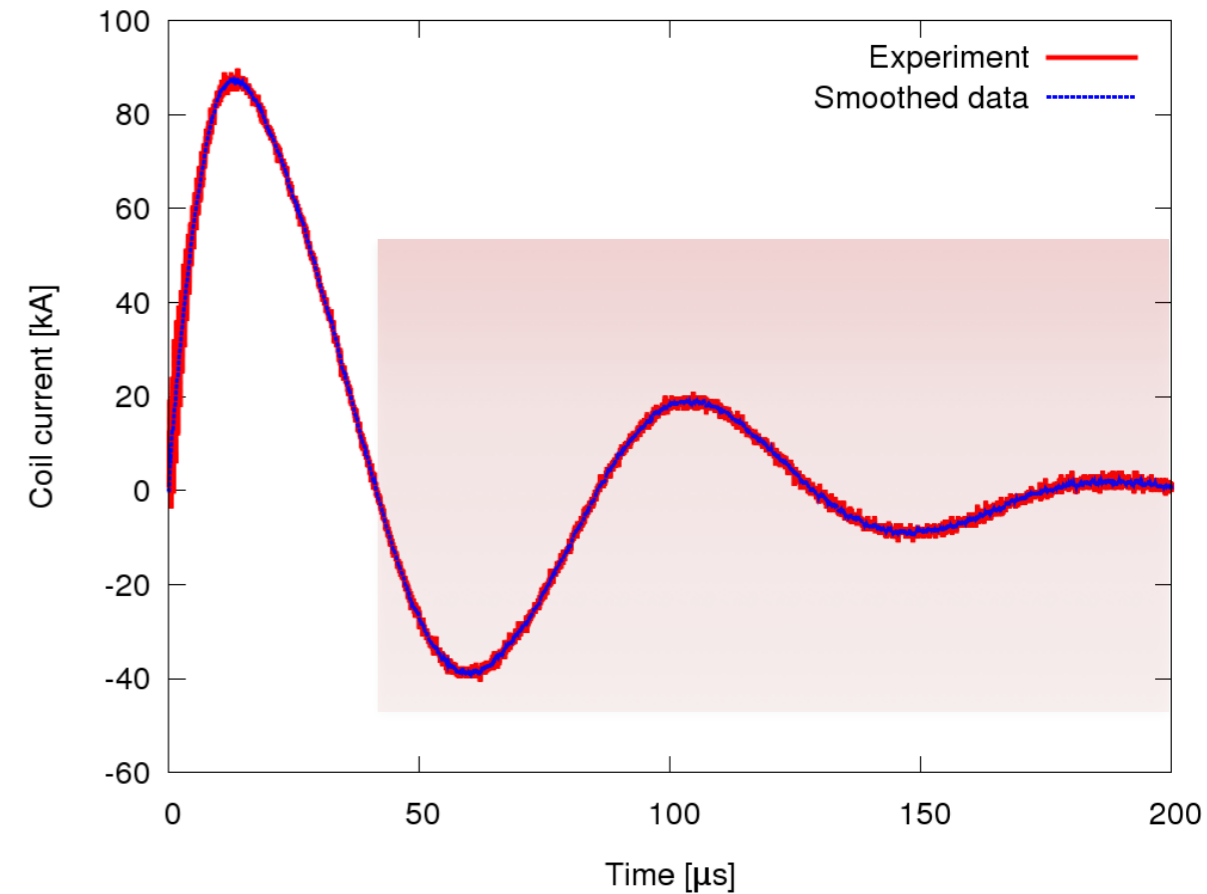
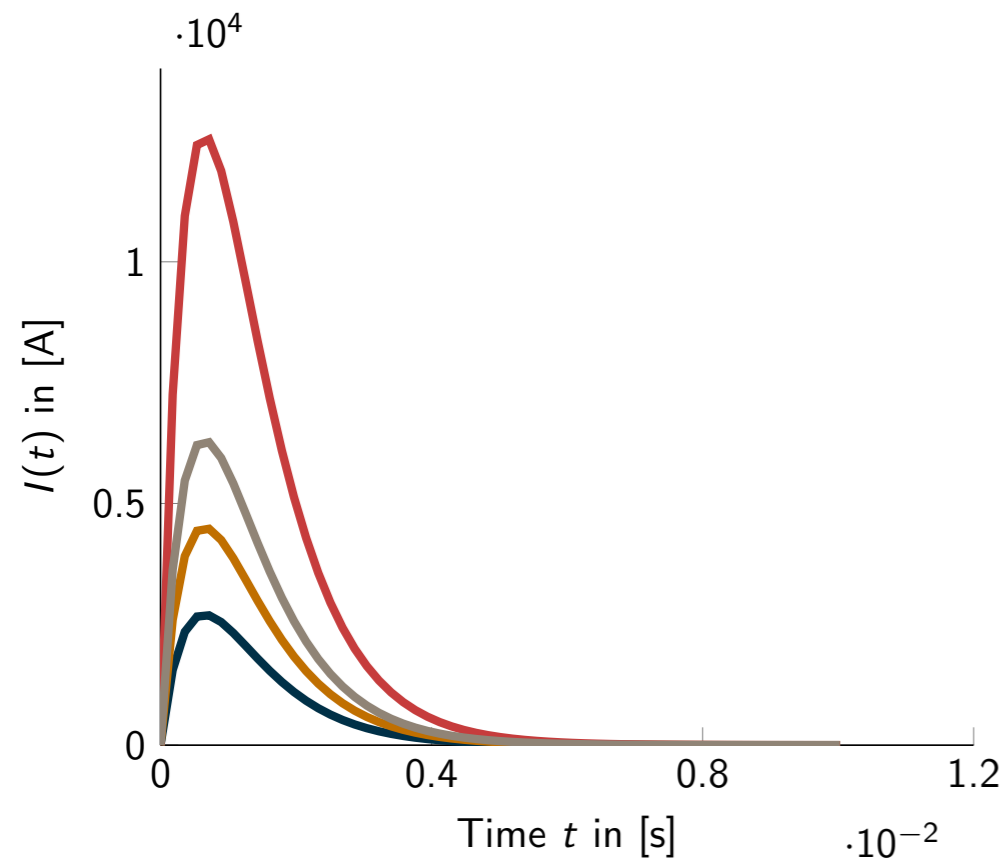


- Only the first half wave is relevant for forming

# Process Optimization in Cup Forming



- Only the first half wave is relevant for forming  
→ Remaining energy absorbed by coils
- Try novel approach to reduce wear and energy consumption



- Only the first half wave is relevant for forming  
→ Remaining energy absorbed by coils
- Try novel approach to reduce wear and energy consumption  
→ Double exponential pulse

$$I(t) = I_{\alpha} e^{-\alpha t} + I_{\beta} e^{-\beta t}$$



# Process Optimization in Cup Forming

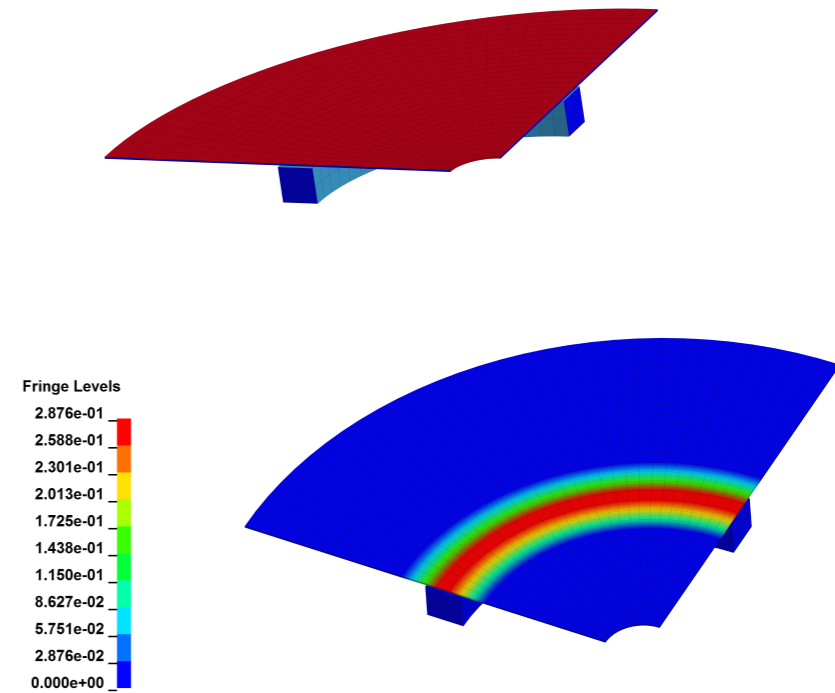
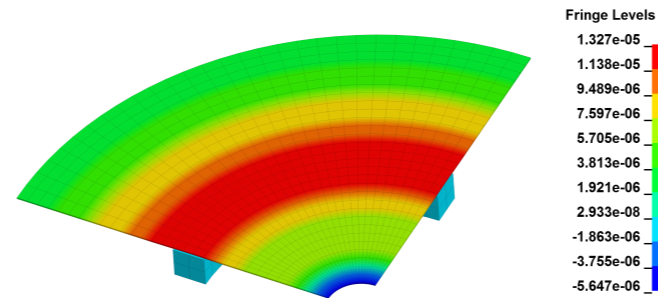
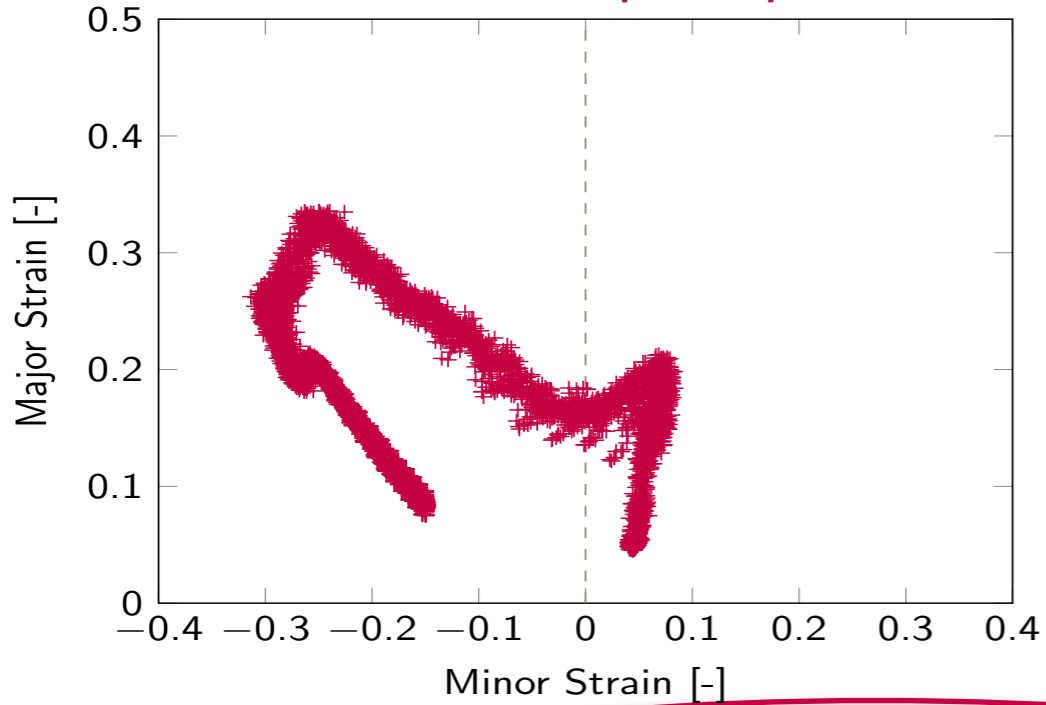
# Process Optimization in Cup Forming

- Maximize the radius at bottom edge



# Process Optimization in Cup Forming

- Maximize the radius at bottom edge
- Maximize the first principle strain



$$\min_{(l_\alpha, l_\beta, \alpha, \beta)^T \in \mathbb{R}^4} - \sum_{j=1}^m \varepsilon_1^j(l_\alpha, l_\beta, \alpha, \beta),$$

subject to  $D_j(l_\alpha, l_\beta, \alpha, \beta) \leq 1 - p, \quad \forall j = 1, \dots, m,$

$$l_\alpha e^{-\alpha t_i} + l_\beta e^{-\beta t_i} \leq l_{\max}, \quad \forall i = 1, \dots, N.$$

# Process Optimization in Cup Forming

- Maximize the radius at bottom edge  
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→ Constrain the damage variable in all elements

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- Current must be technically reasonable  
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$$\min_{(I_\alpha, I_\beta, \alpha, \beta)^T \in \mathbb{R}^4} - \sum_{j=1}^m \varepsilon_1^j(I_\alpha, I_\beta, \alpha, \beta),$$

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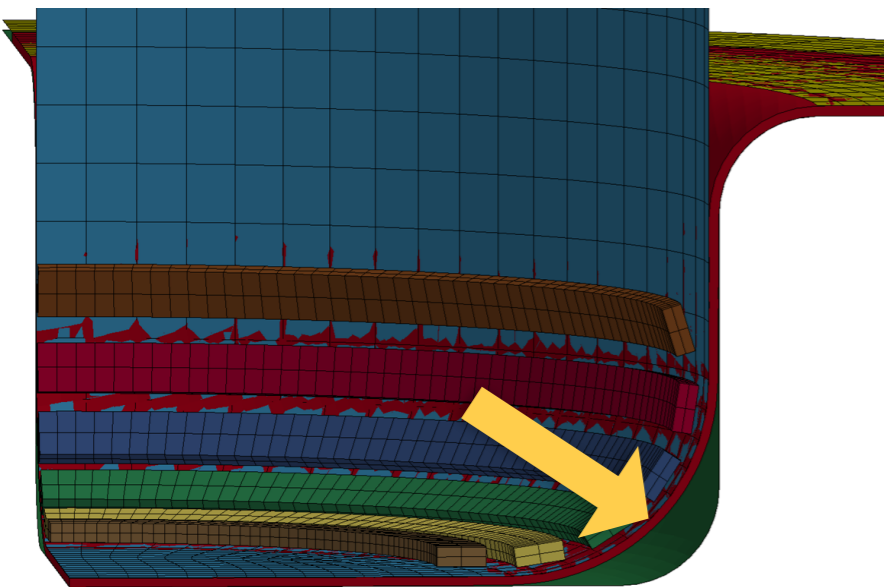
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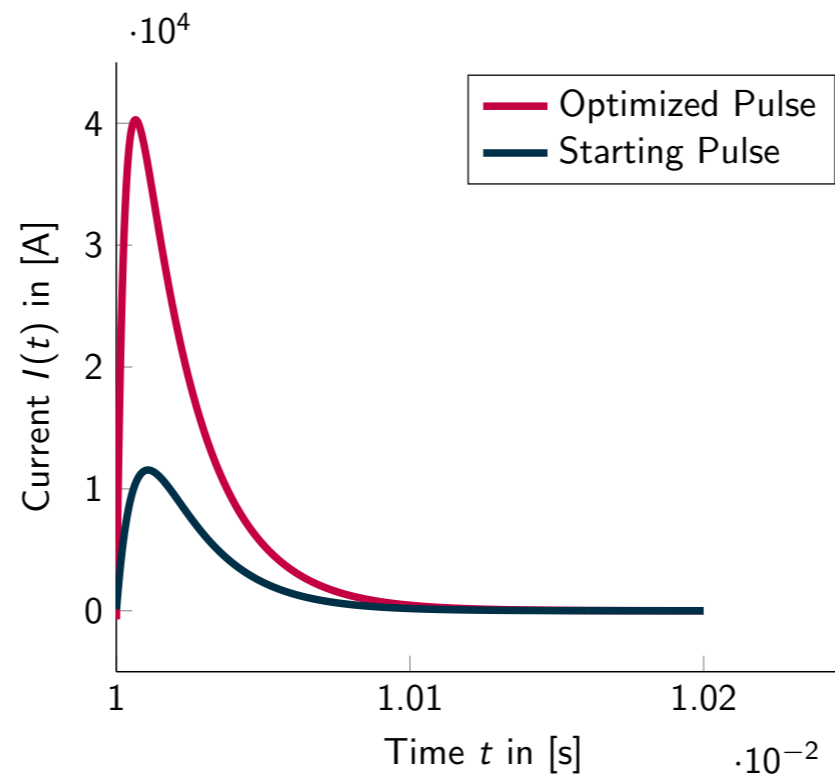
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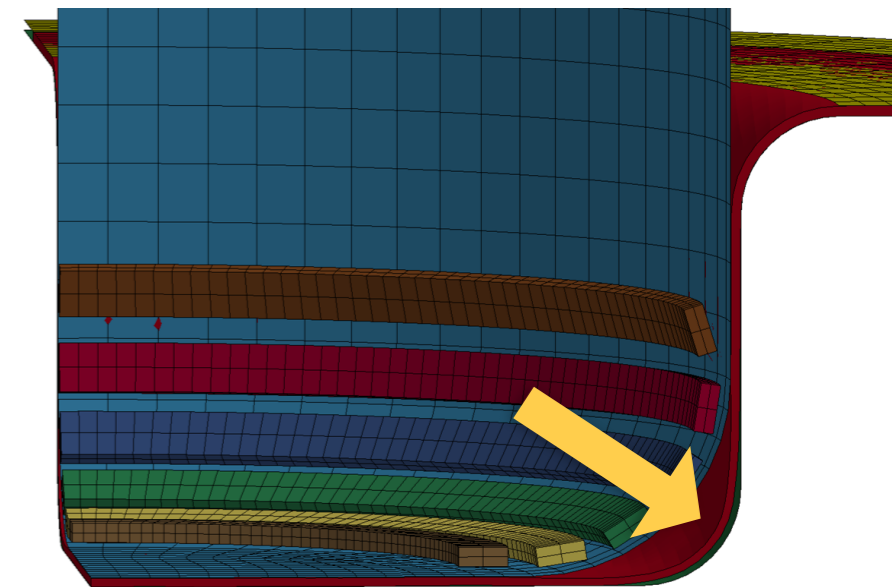
# Results



$r = 20 \text{ mm}$   
 $d = 0.91 \text{ mm}$



$I_\alpha = -65570.2 \text{ A}$   
 $I_\beta = 64867.8 \text{ A}$   
 $\alpha = 6878.78$   
 $\beta = 973.021$



$r = 15.35 \text{ mm}$   
 $d = 0.85 \text{ mm}$

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  - ✓ Linearization based scheme for process parameter identification
- First steps have been taken, but:
  - ➔ Verification of computed process parameters by experiments
  - ➔ Taking into account more process parameters at the same time, control of quasi-static part and electromagnetic part simultaneously



# Special thanks to:



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(Leibnitz University Hannover)



Department of the Theory of Electrical Engineering  
(Helmut Schmidt University Hamburg)



Institute for Applied Mechanics  
(RWTH Aachen)